

# Lab on a Chip and Microfluidics

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l'institut  
d'électronique



# Part X. Capillarity and Wetting

# Capillarity and Wetting



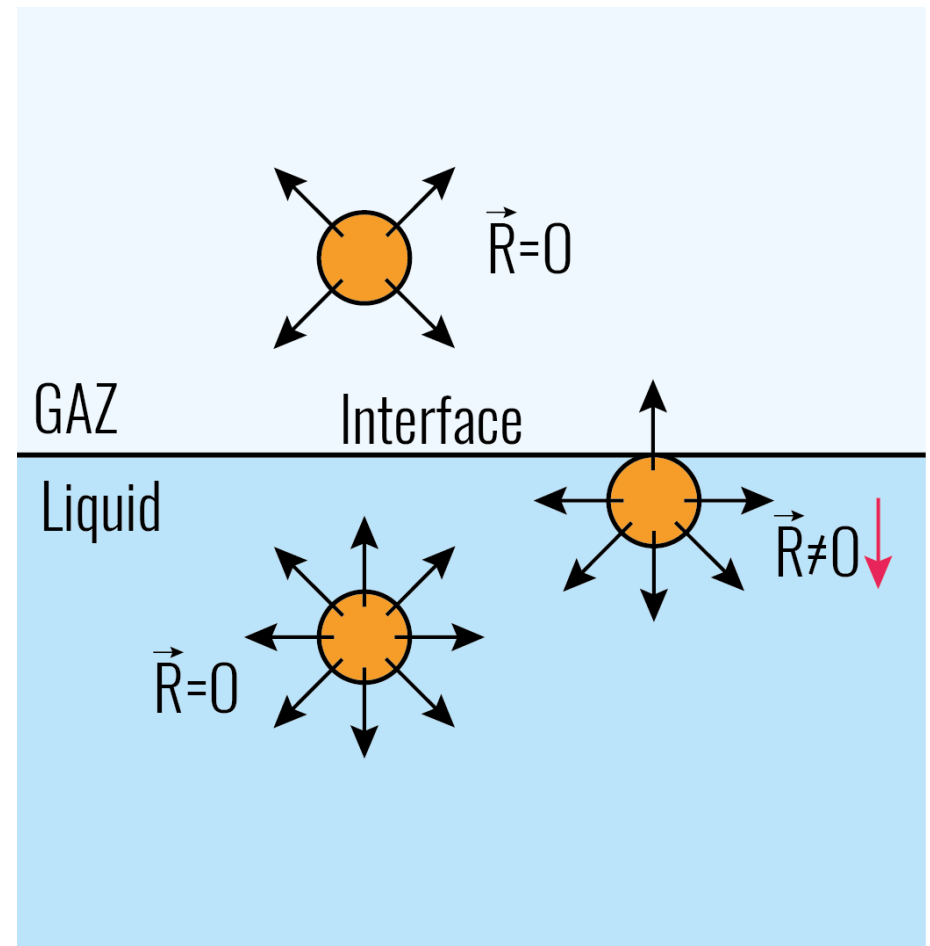
# Surface Tension

The superficial layer of a liquid is submitted to a force that tends to lower this surface : it is the Surface Tension

Greater attraction of liquid molecules to each other than to the molecules in the air

$$E_s = \gamma S$$

$$[\gamma] = J / m^2 = N / m$$

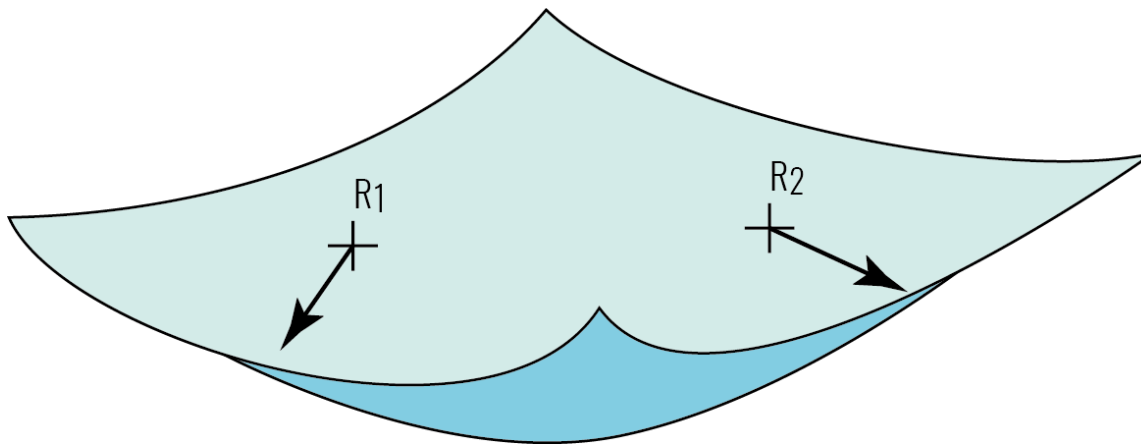


Water	72,8	$10^{-3} \text{ N.m}^{-1}$
Ethanol	22,2	
Acetone	23	
Blood	60	
Liquid Nitrogen	8,8	
Mercury	<b>486</b>	

# Surface Tension : Young Laplace

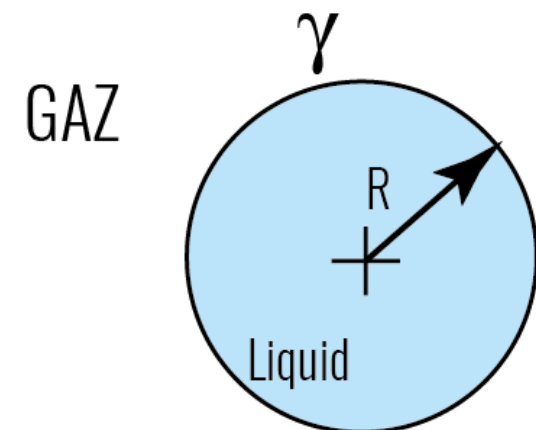
The bending of a liquid/gaz interface produces a pressure difference between each sides of the interface such as :

$$\Delta P = \gamma \cdot \text{div}(\vec{n}) = \gamma \left( \frac{1}{R_1} + \frac{1}{R_2} \right)$$



For a sphere (one curvature radius) :

$$\Delta P = \frac{2\gamma}{R}$$



# Surface Tension : Young Laplace

Droplet of water in the air

$$\Delta P = \frac{2\gamma}{R}$$



Soap bubble

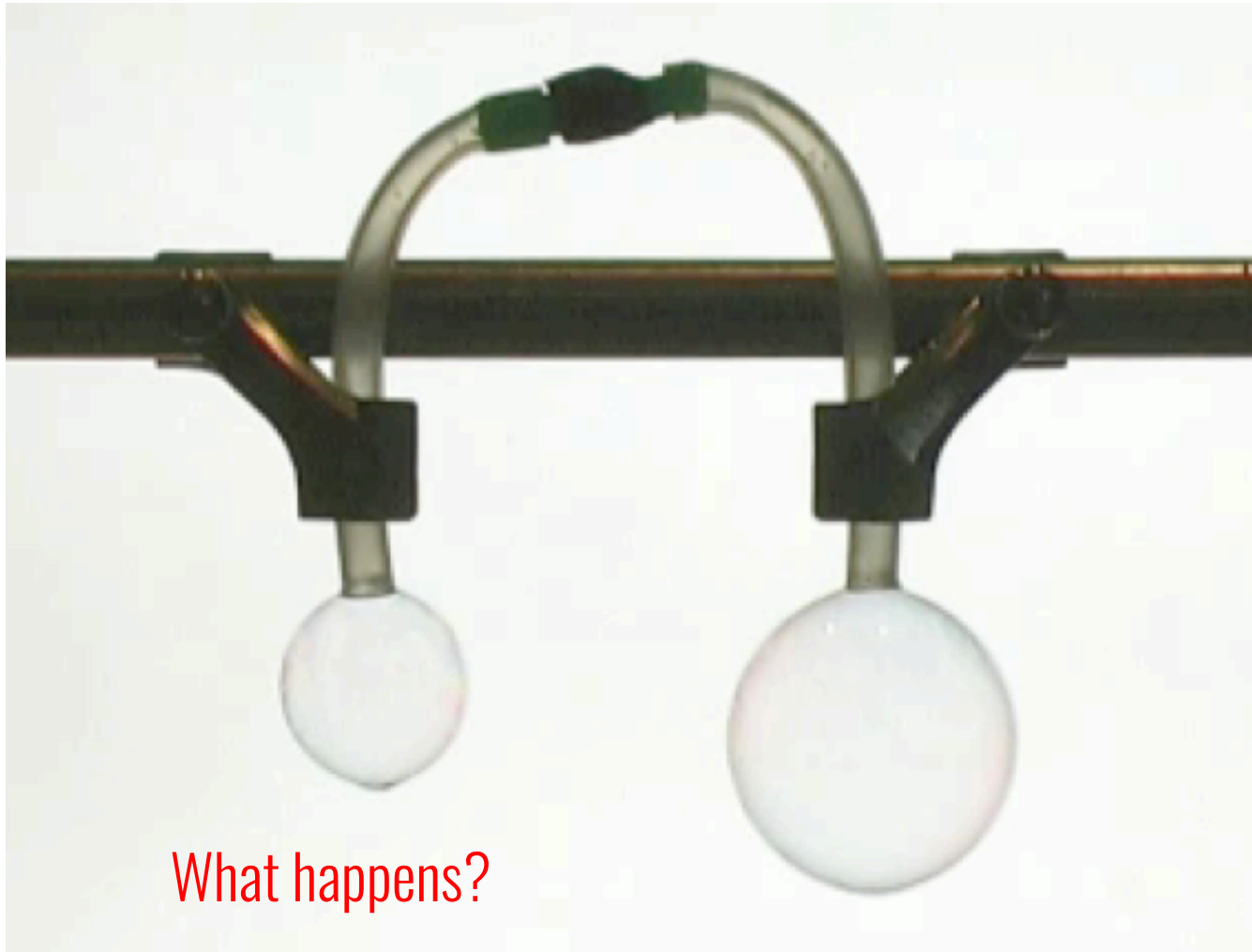


$$\Delta P = \frac{4\gamma}{R}$$

Why 4?

# Surface Tension : Young Laplace

Two connected balloons experiment



# Surface Tension : liquid metal

Liquid Gallium droplet coalescence

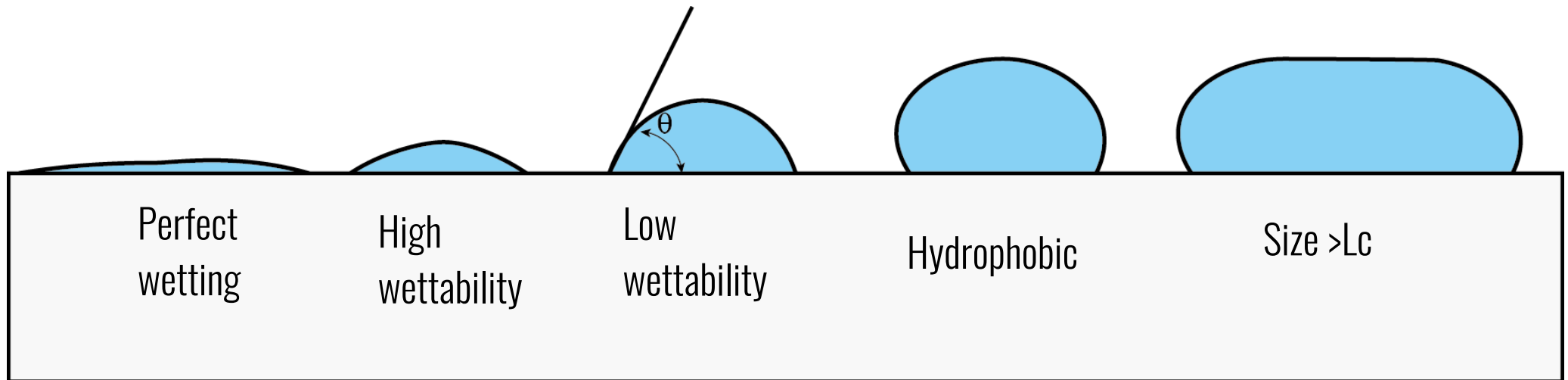




# Wetting

Now, Three phases :  
Solid / Liquid / Gaz

Wetting is the balance between  
cohesive and adhesive forces



# Capillary length

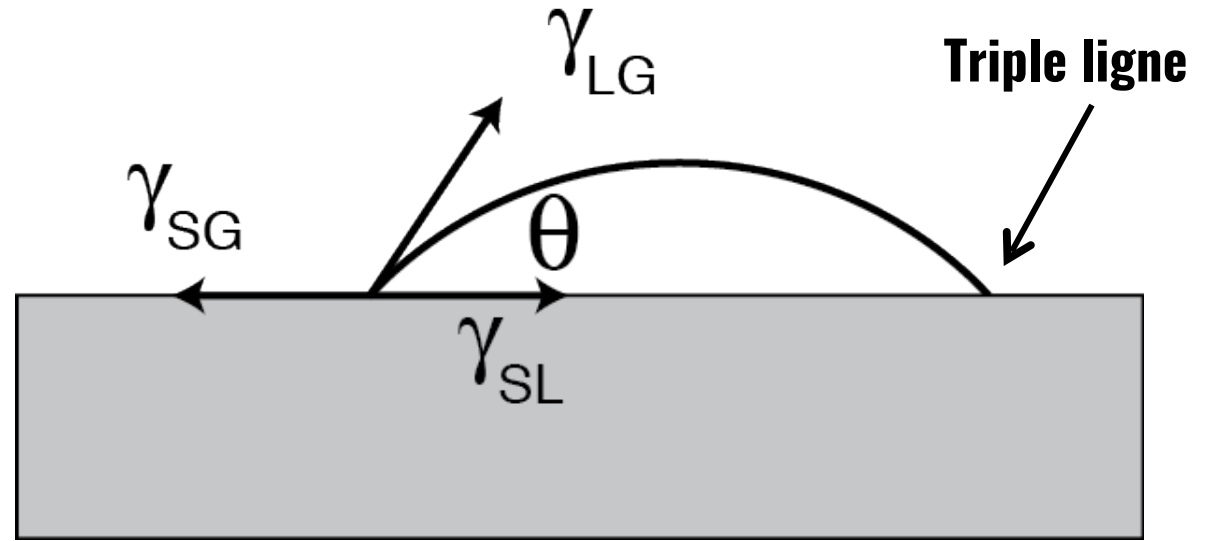
$$L_c = \frac{\gamma}{\rho g}$$

$\gamma$  is the surface tension  
 $\rho$  is the density of the liquid  
 $g$  is the gravitational acceleration

# Wetting : Young Dupré

Young-Dupré law

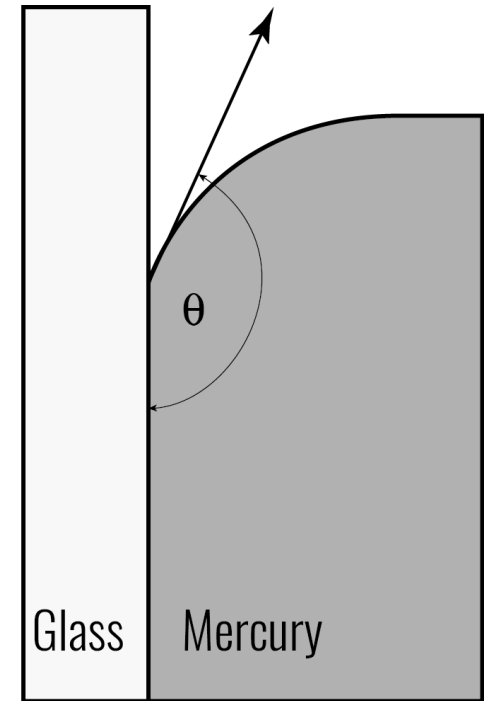
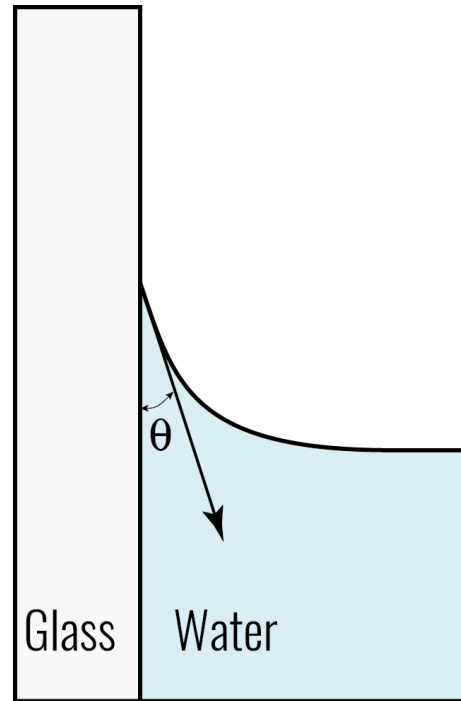
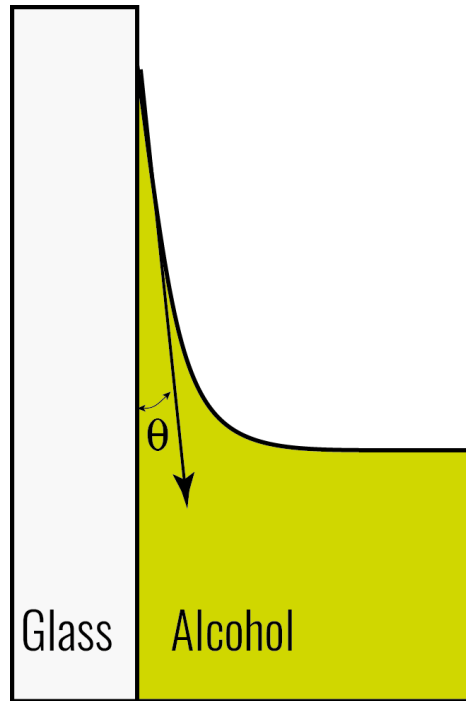
$$\cos \theta = \frac{\gamma_{SG} - \gamma_{SL}}{\gamma_{LG}}$$



Wetting angles

Water on SiO <sub>2</sub>	52,3°
Water on Glass	25°
Water on Gold	0°
Water on Platinum	40°
Water on PMMA	73,7°
Water on PDMS	100°
Mercury on Glass	140°

# Wetting : Meniscus



# Wetting : Larmes du vin

## Marangoni effect

mass transfer along an interface between two fluids due to surface tension gradient.

A liquid with a high surface tension pulls more strongly on the surrounding liquid than one with a low surface tension

## Marangoni number

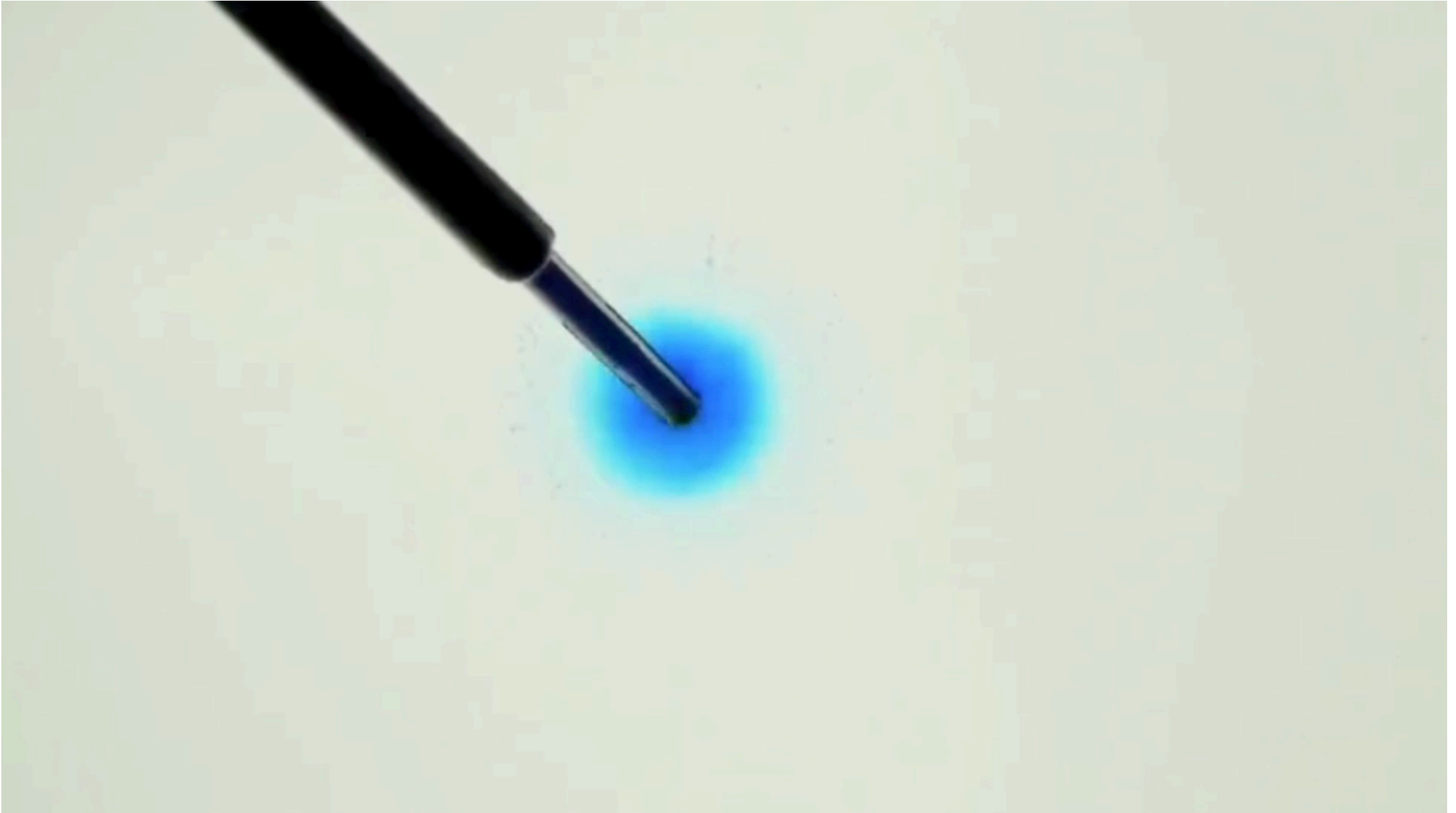
$$\text{Ma} = -(\partial\gamma/\partial T) \cdot \frac{L \cdot \Delta T}{\eta \cdot \alpha}$$

Par Epop — Travail personnel, Domaine public, <https://commons.wikimedia.org/w/index.php?curid=4528610>

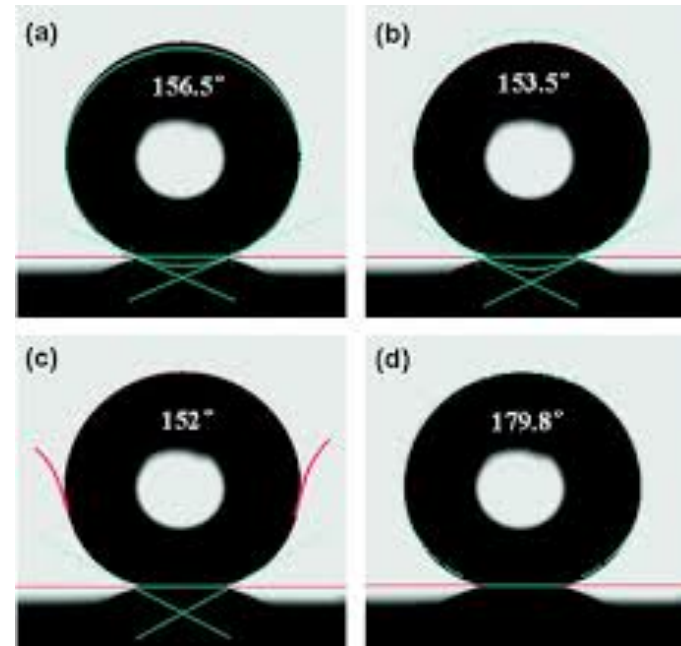
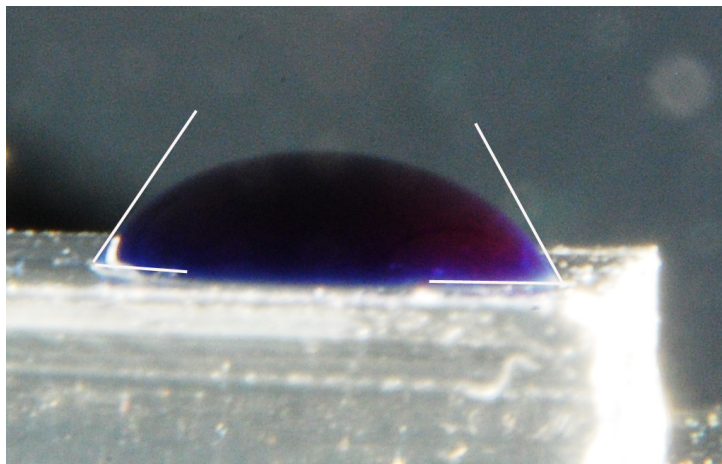
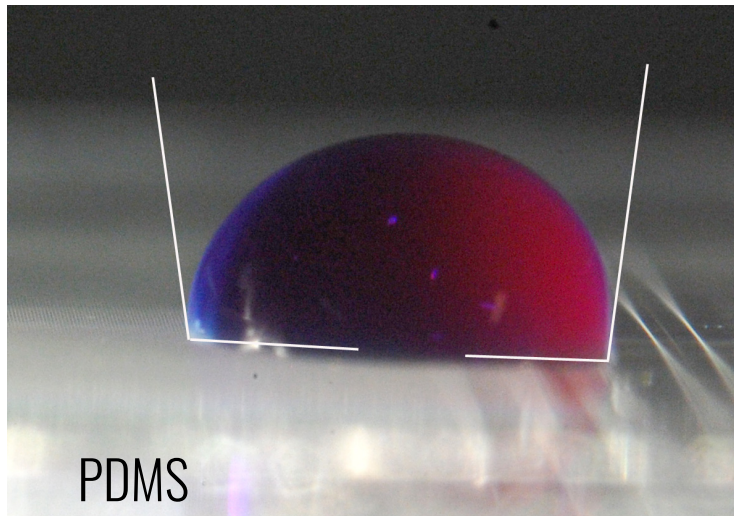


# Wetting

Marangoni effect

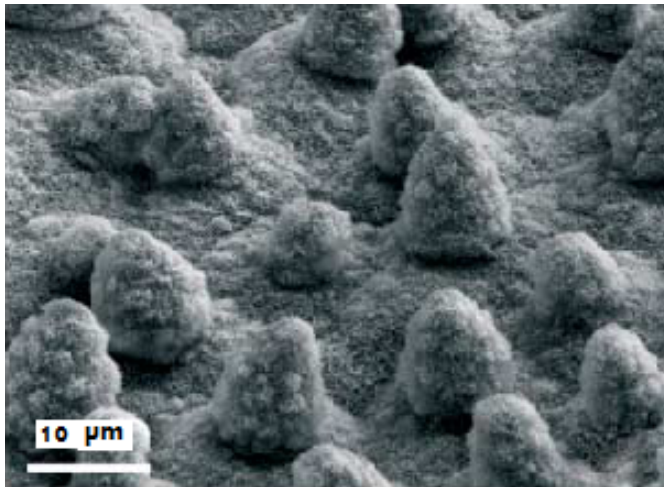


# Hydrophobicity

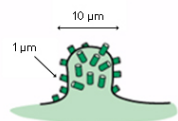
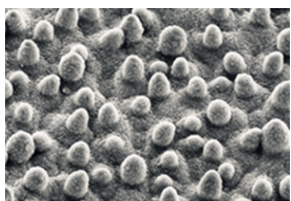
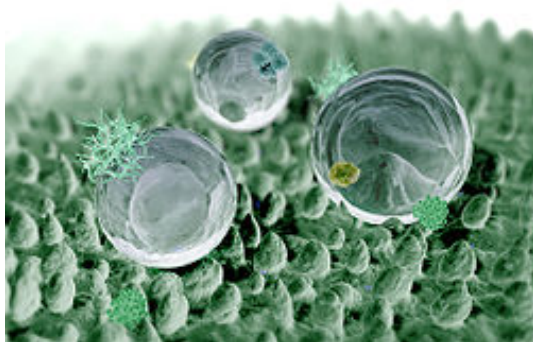


Mercury

# Super Hydrophobicity



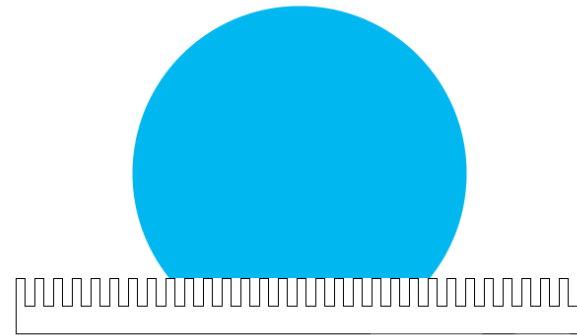
Lotus



Wenzel and Cassie-Baxter models

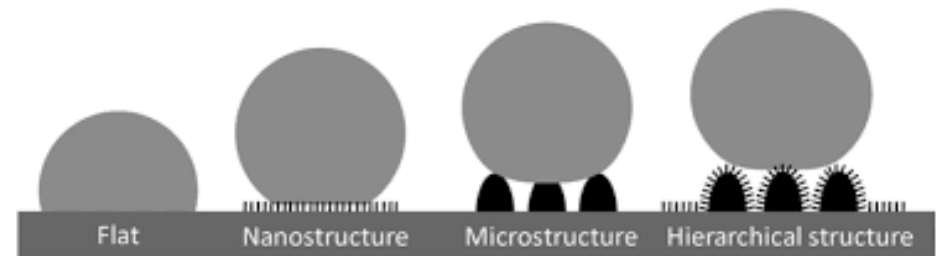


Wenzel : état « empalé »



Cassie-Baxter: état « fakir »

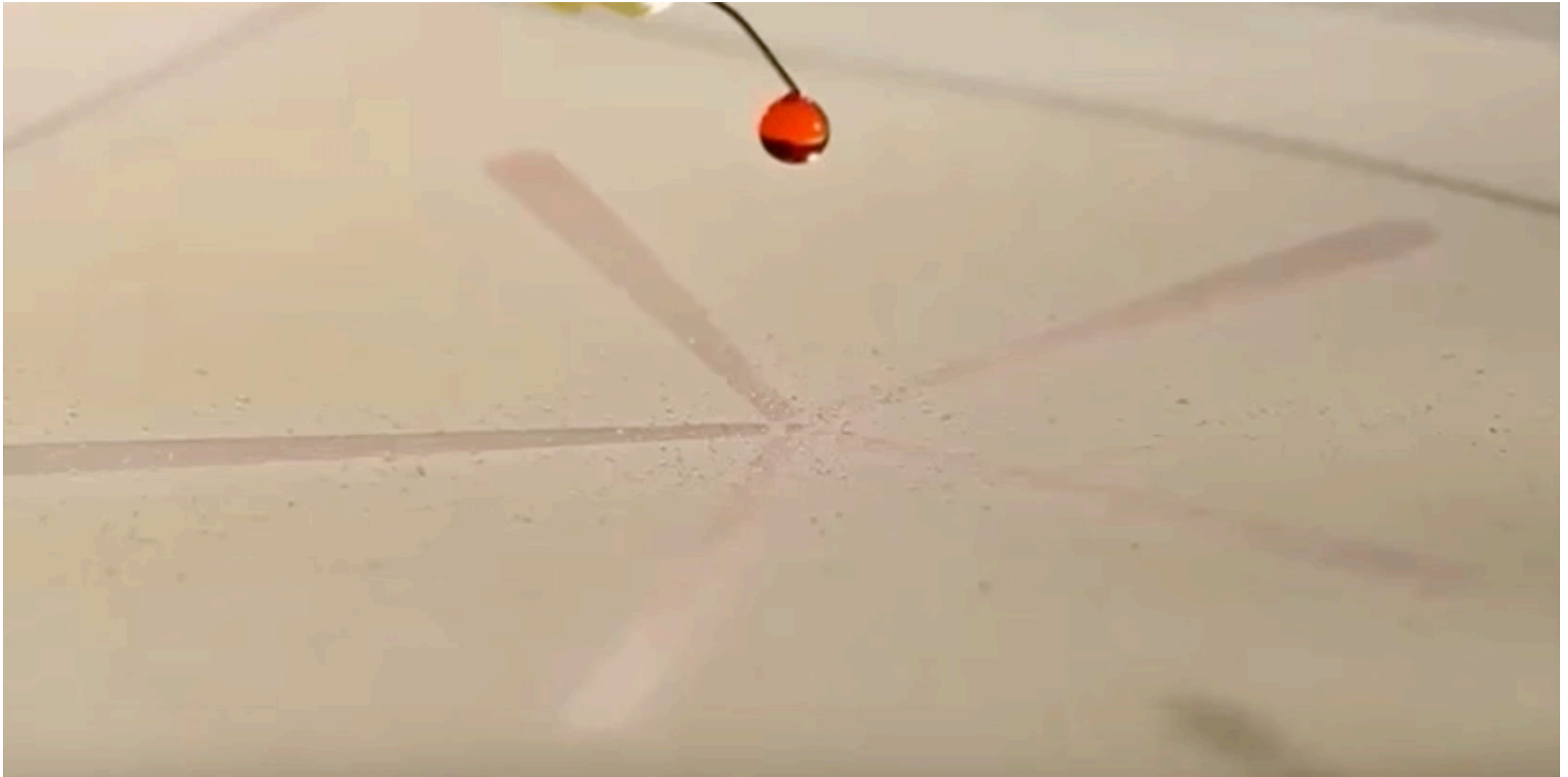
Wetting of four different surfaces



# Super Hydrophobicity

Hydrophilic patterns on a hydrophobic surface

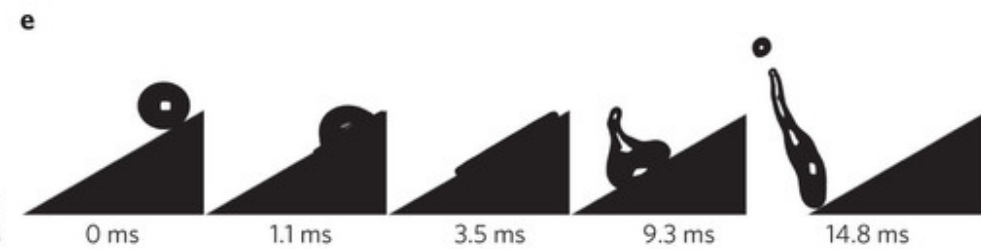
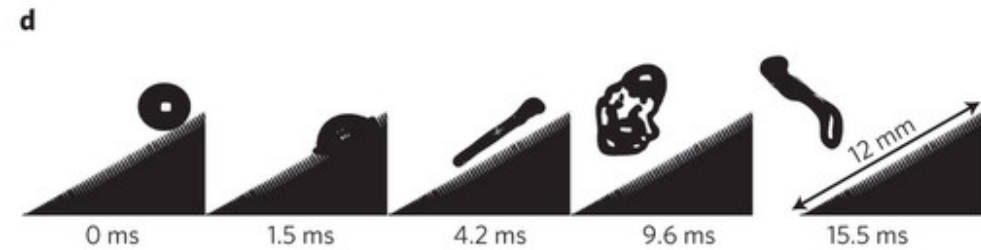
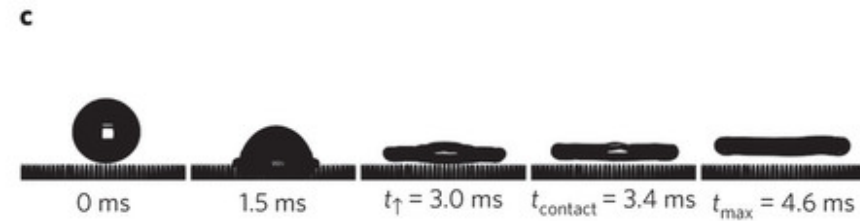
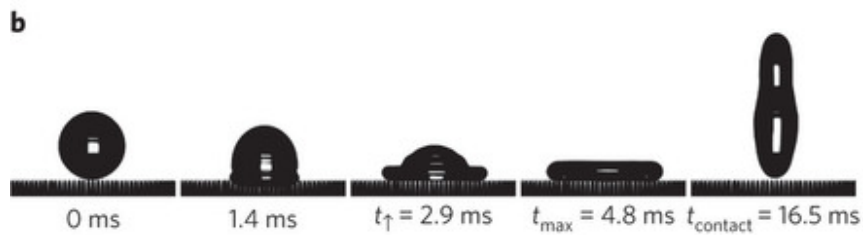
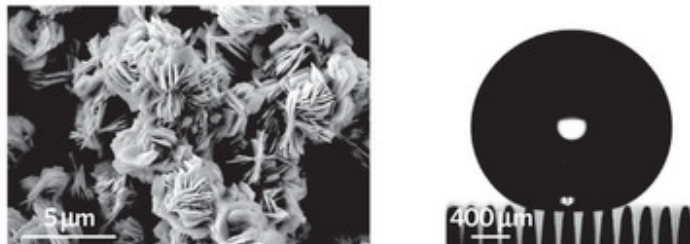
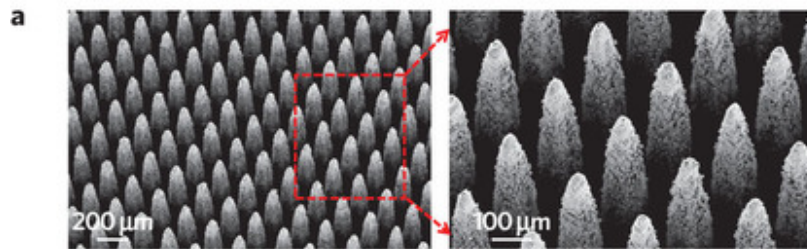
Constantine M. Megaridis, Aritra Ghosh, Ranjan Ganguly, Mechanical and Industrial Engineering, University of Illinois at Chicago





# Super Hydrophobicity

Dynamique des gouttes, rebonds



# Capillary number

$$C_a = \frac{v\mu}{\gamma}$$

$\gamma$  est la tension superficielle du liquide ;  
 $v$  est la vitesse du liquide  
 $\mu$  est la viscosité dynamique;

# Capillary length

$$L_c = \frac{\gamma}{\rho g}$$

$\gamma$  est la tension superficielle du liquide ;  
 $\rho$  est la masse volumique du liquide  
 $g$  est l'accélération gravitationnelle

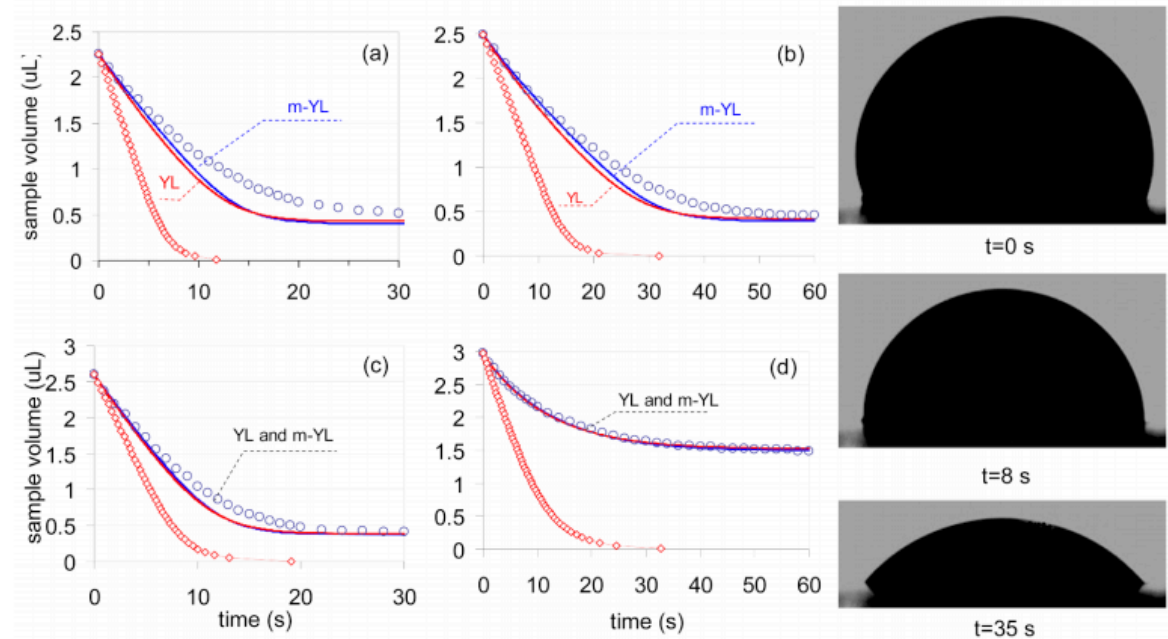
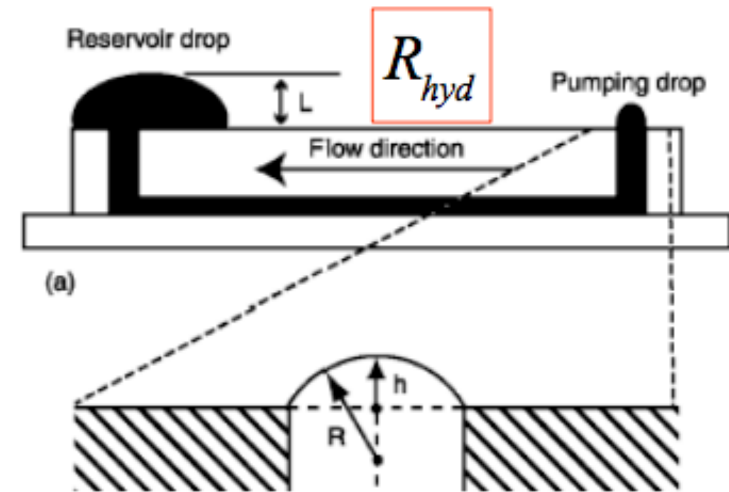
# Capillary Pumps

Application : Pumping without mechanics

$$\Delta p = \frac{2\gamma}{R}$$

$$Q = \frac{\Delta p}{R_{hydro}} = \frac{dVol}{dt}$$

$$t_{disparition} \approx \frac{R_{hydro} R_0^4}{\gamma}$$



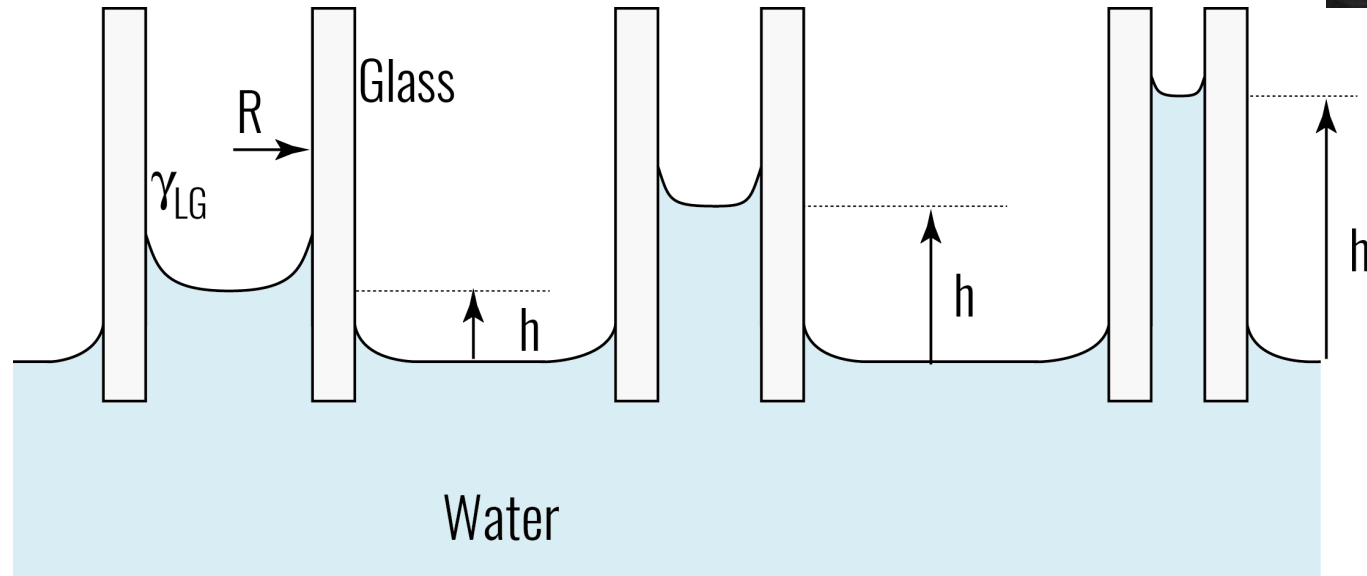
# Jurin's law

James Jurin (baptisé le 15 décembre 1684 – 29 mars 1750) est un médecin et physicien anglais passé à la postérité pour ses travaux pionniers relatifs à l'action capillaire et à l'épidémiologie (variolisation). Il fut l'un des plus chauds partisans des travaux d'Isaac Newton et mit tout son talent de satiriste au service de ses idées.



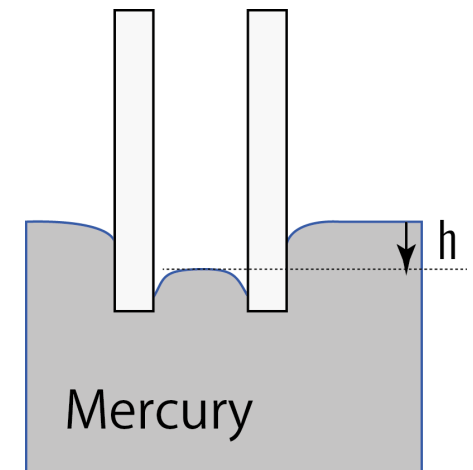
Jurin's law describes the rise and fall of a liquid within a thin capillary tube.

Competition between depression under the meniscus and weight of the water column



$$h = \frac{2\gamma \cos \theta}{\rho g R}$$

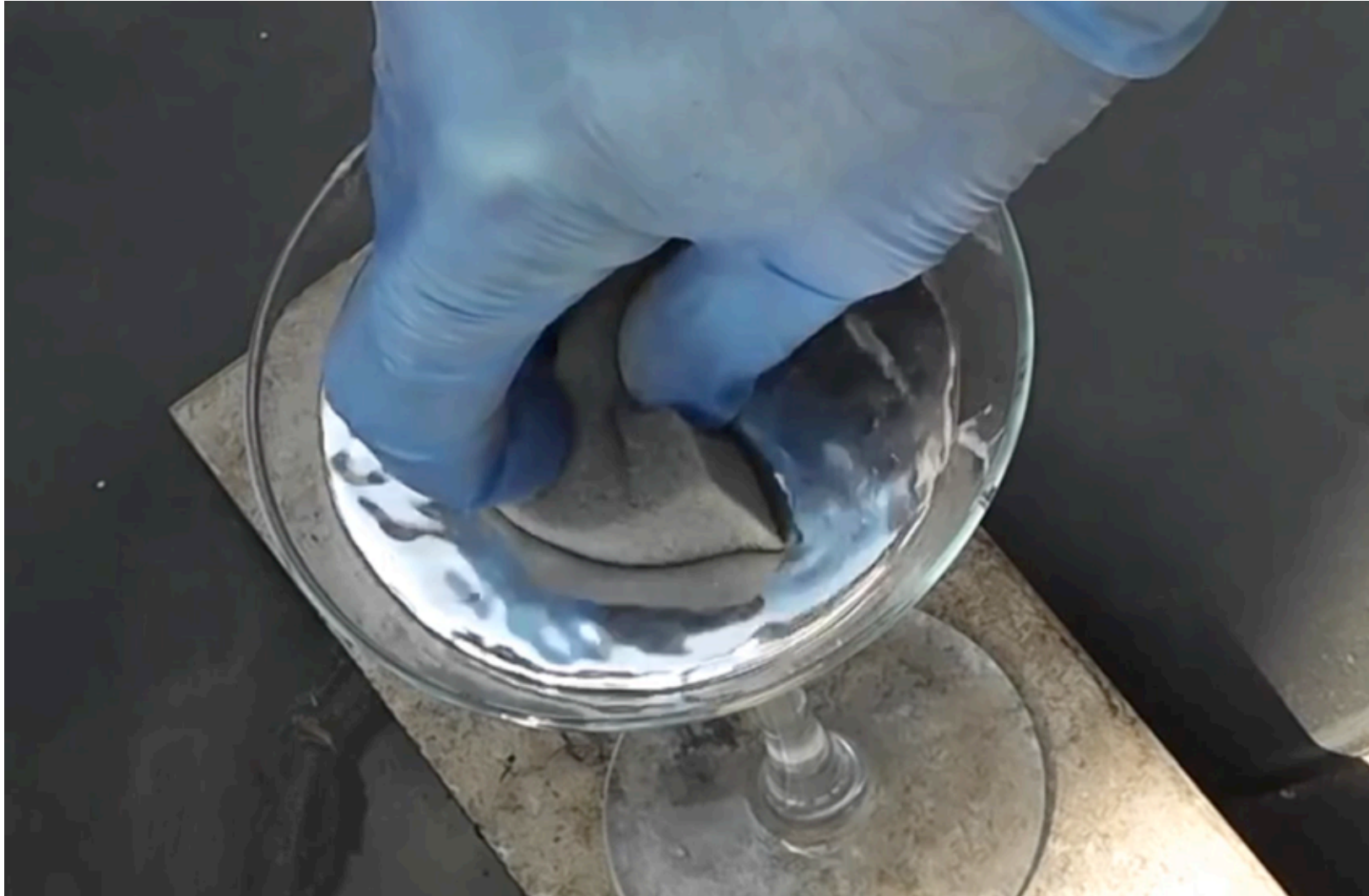
$h$  is the liquid height ;  
 $\gamma$  is the liquid surface tension ;  
 $\theta$  is the contact angle of the liquid on the tube wall ;  
 $\rho$  is the liquid density ;  
 $R$  is the tube radius ;  
 $g$  is the gravitational acceleration.



Valid for  $R < L_c$

# Imbibition

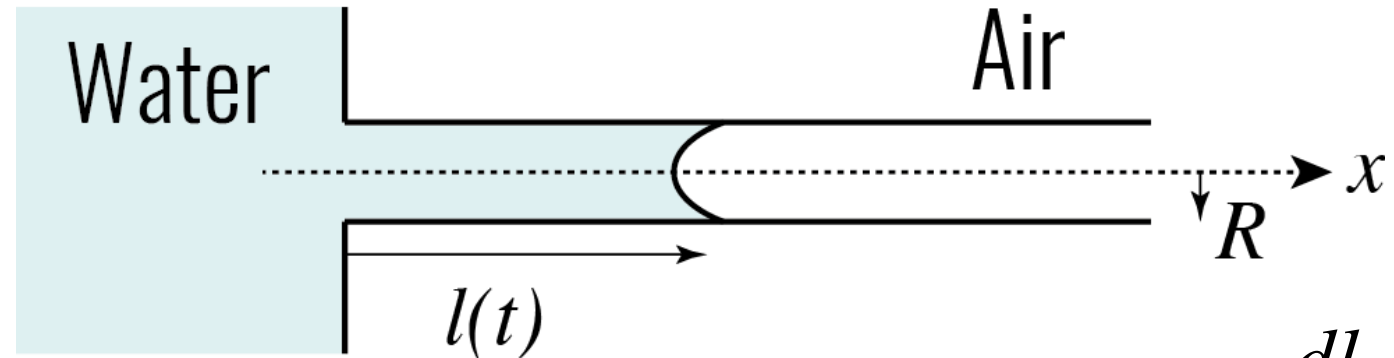
Sponge in mercury : what happens ?



# Imbibition



Flow driven by Laplace pressure



With a Poiseuille flow

$$Q = \pi R^2 v_m = \pi R^2 \frac{dl}{dt}$$

$$v_m = \frac{dl}{dt} = \frac{R^2}{8\mu} \frac{dp}{dx} = \frac{R^2}{8\mu} \frac{\Delta p}{l(t)}$$

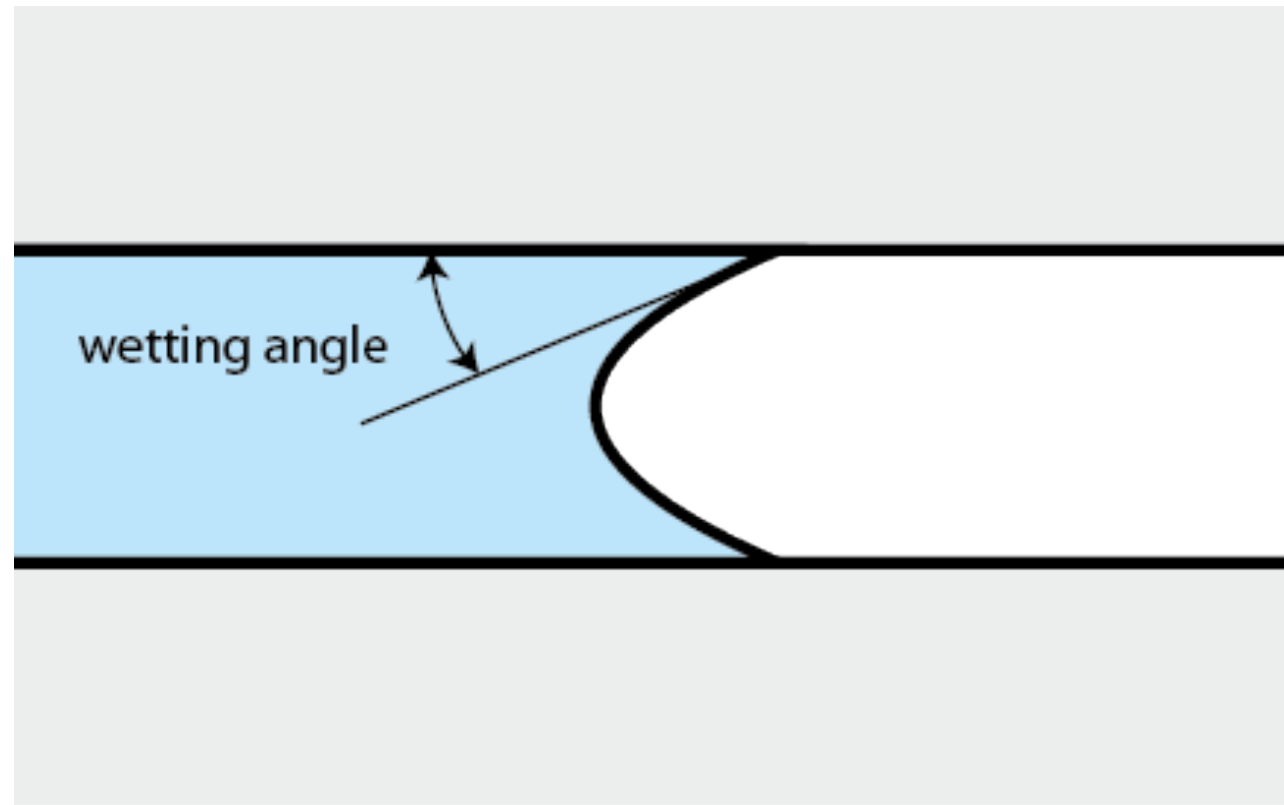
With Young Laplace equation

$$l(t) = \sqrt{\frac{R\gamma \cos(\theta)}{2\mu} t}$$

$$\Delta p = \frac{2\gamma}{R} \cos(\theta)$$

It is the law of Washburn

# Capillary driven microfluidics

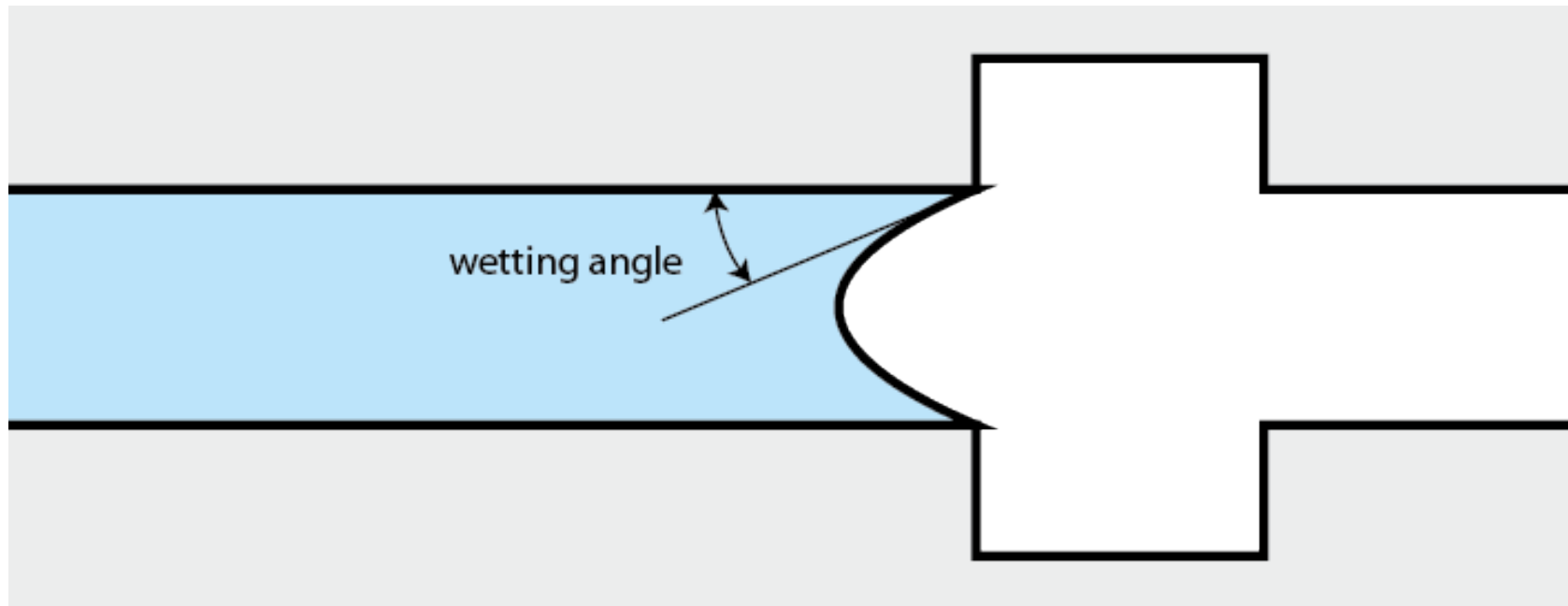


# Capillary driven microfluidics

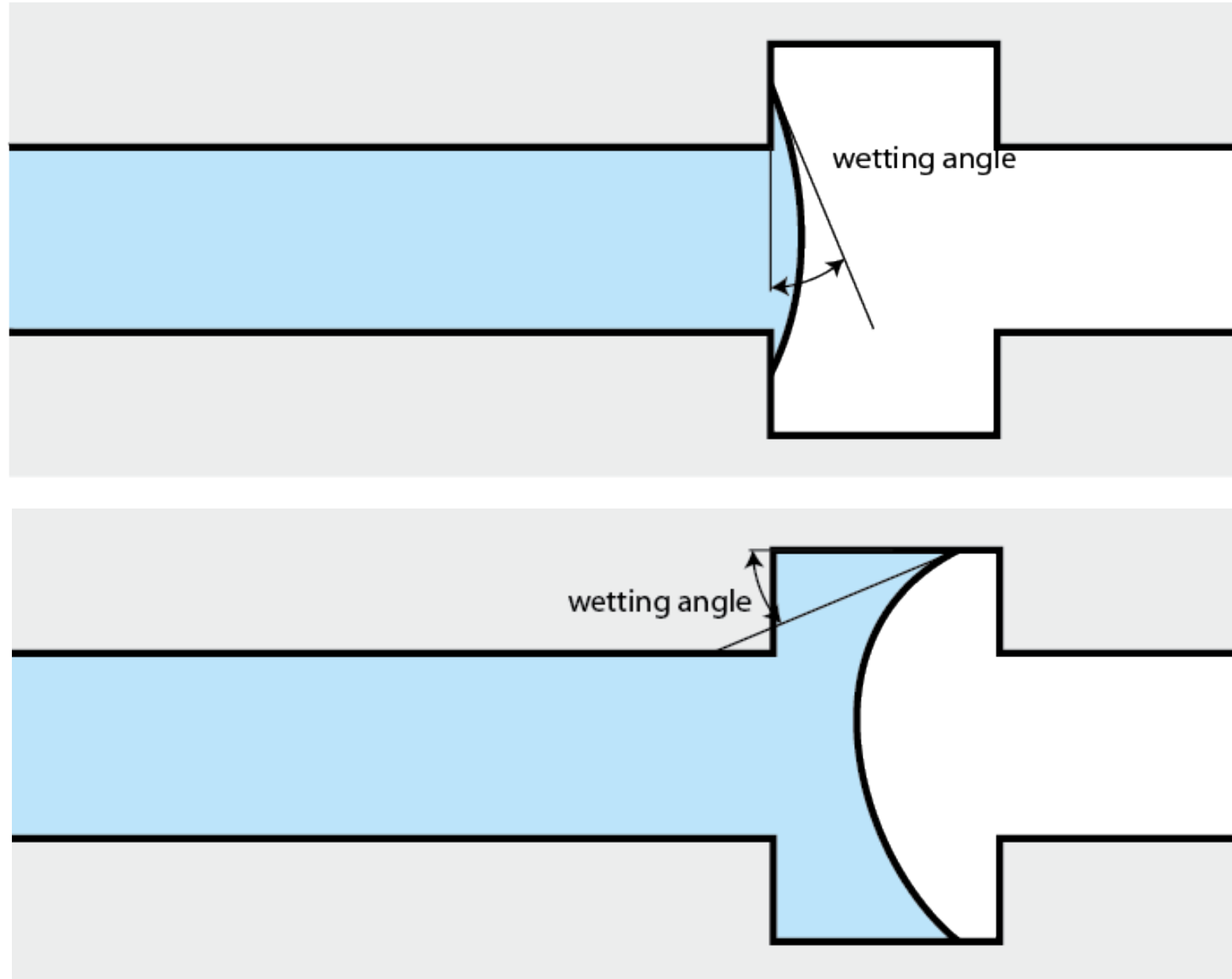




# Capillary driven microfluidics

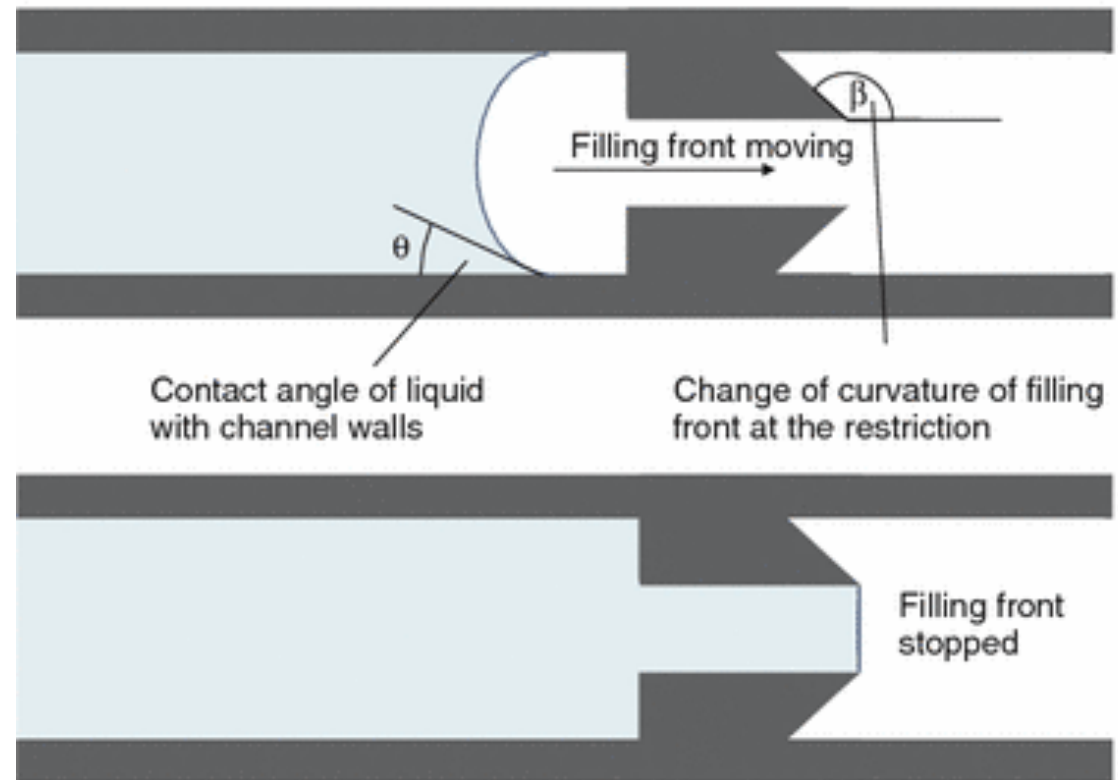


# Capillary driven microfluidics



# Stop valves

**(a)** Principle of a stop valve

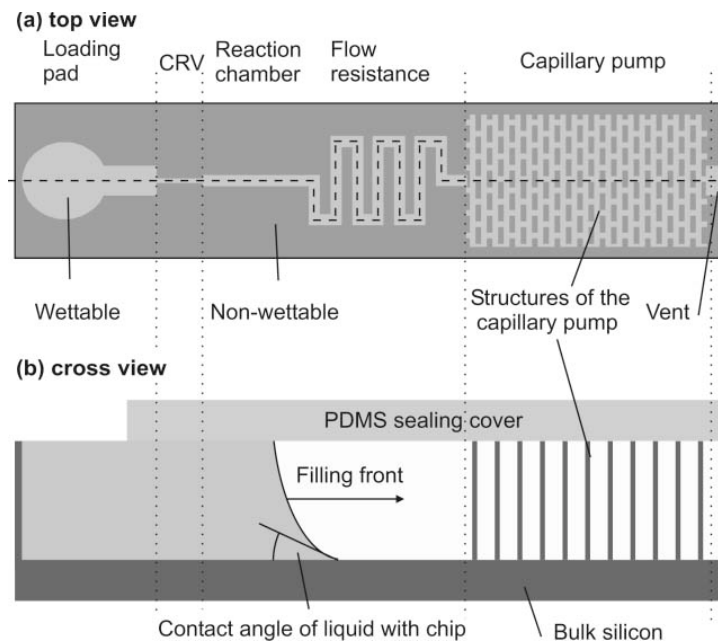
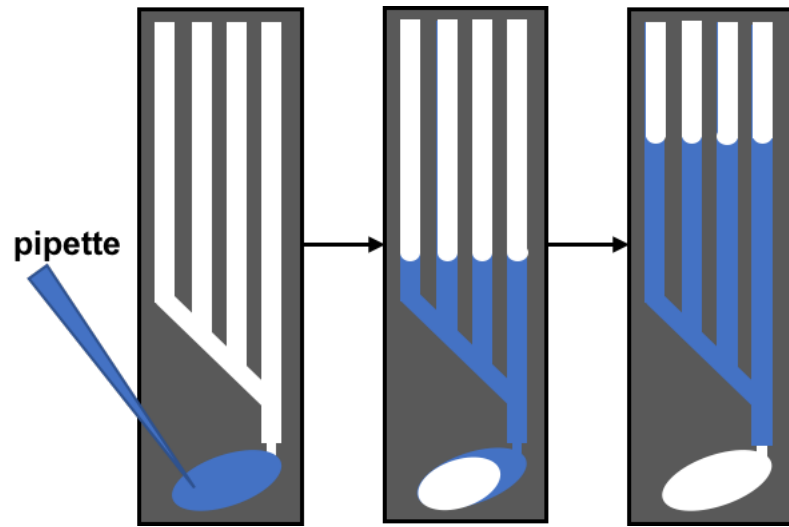


**(b)** Stop valves etched in silicon

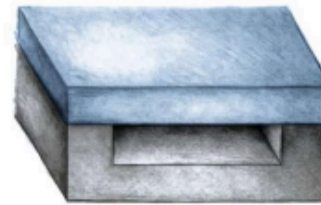


150  $\mu\text{m}$

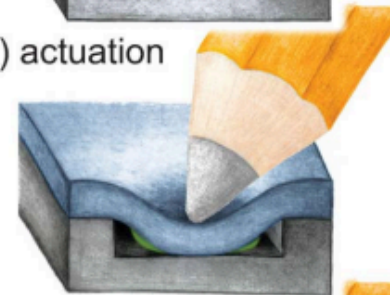
# Capillary driven microfluidics



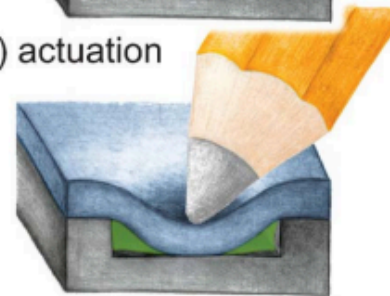
(a) closed



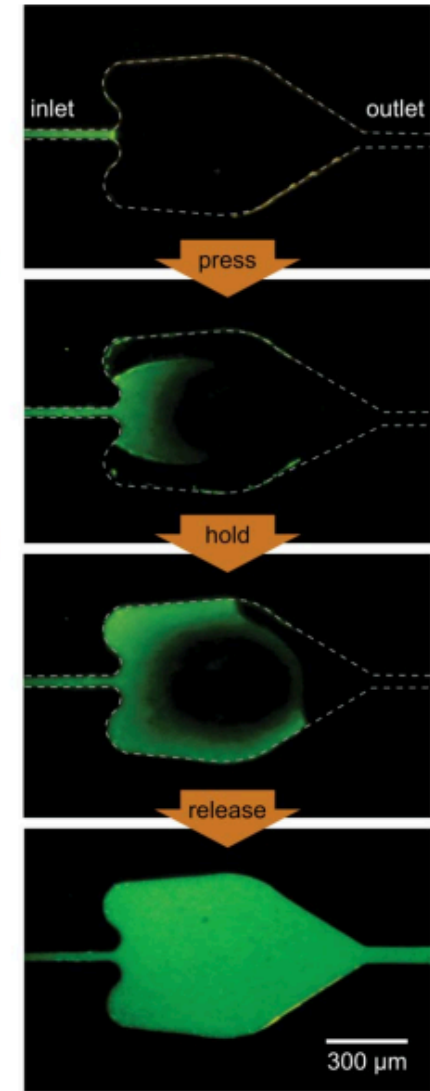
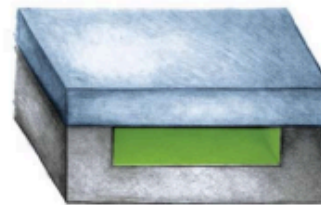
(b) actuation



(c) actuation

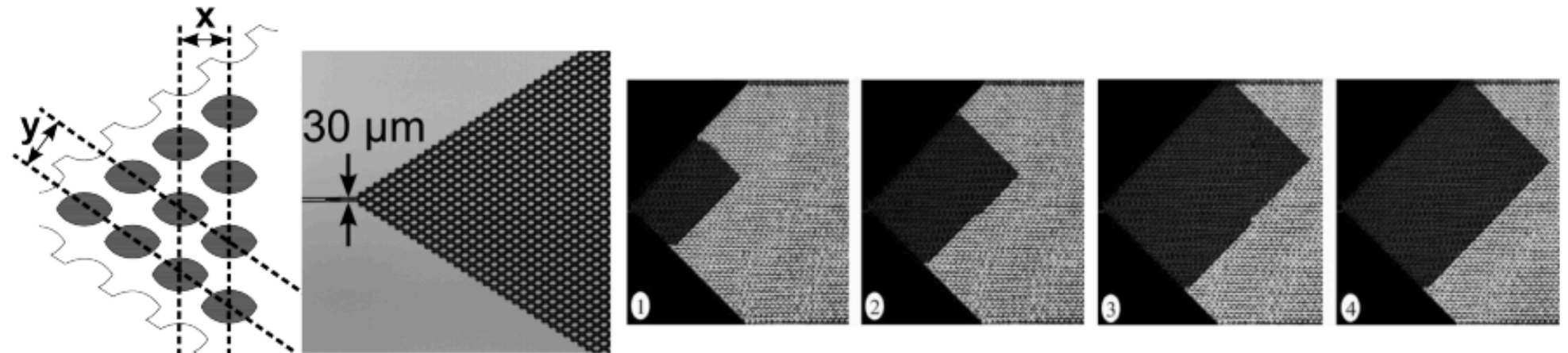


(d) open



# Capillary driven microfluidics

(f) capillary pump



$$P_c = -\gamma \left( \frac{\cos \theta_b + \cos \theta_t}{d} + \frac{\cos \theta_l + \cos \theta_r}{w} \right)$$

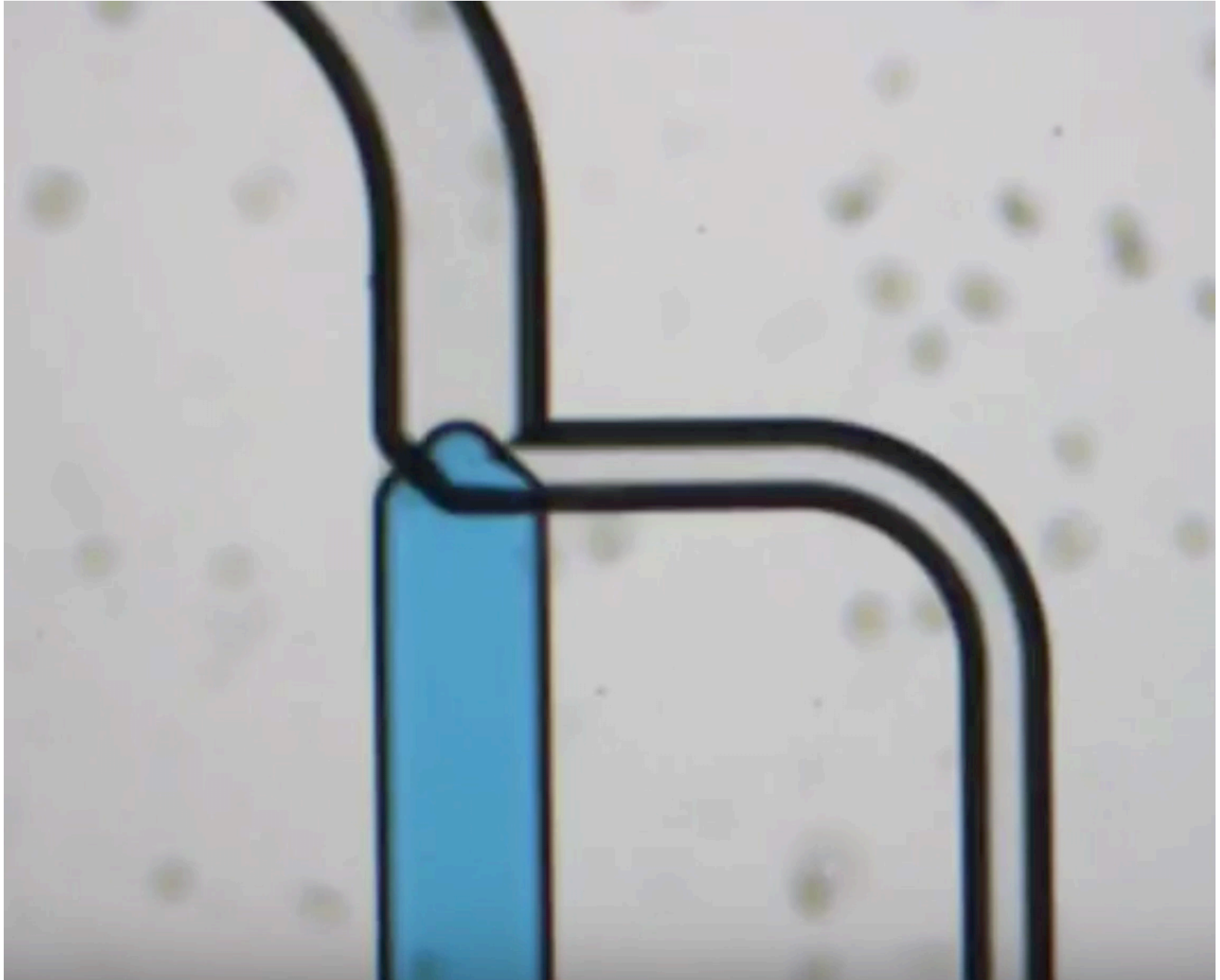
$$R_{FR} = \left[ \frac{1}{12} \left( 1 + \frac{5a}{6b} \right) \frac{AR_H^2}{L} \right]^{-1} \quad R_H = \frac{2A}{P} \quad D = \frac{1}{\eta} \frac{\Delta P}{R_{FR}}$$

$a$  and  $b$ : width or depth,  $b > a$

# Capillary driven microfluidics



# Capillary driven microfluidics



# Capillary driven microfluidics

Video related to research article  
appearing in *Lab on a Chip*

Roosbeh Safavieh and David Juncker

“Capillarics: Pre-Programmed, Self-Powered  
Microfluidic Circuits Built From Capillary  
Elements”

Read the article at

<http://pubs.rsc.org/en/content/articlelanding/2013/lc/C3LC50691F>



# Capillary driven microfluidics

Dehydration and rehydration of reagents

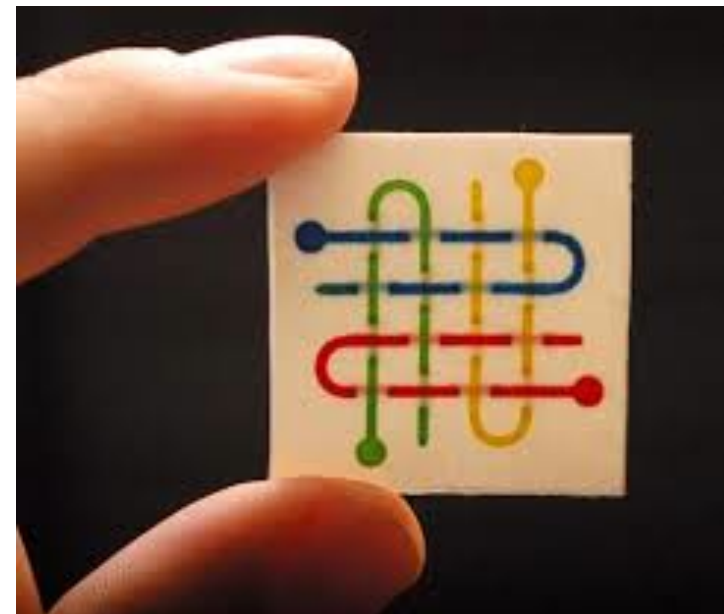
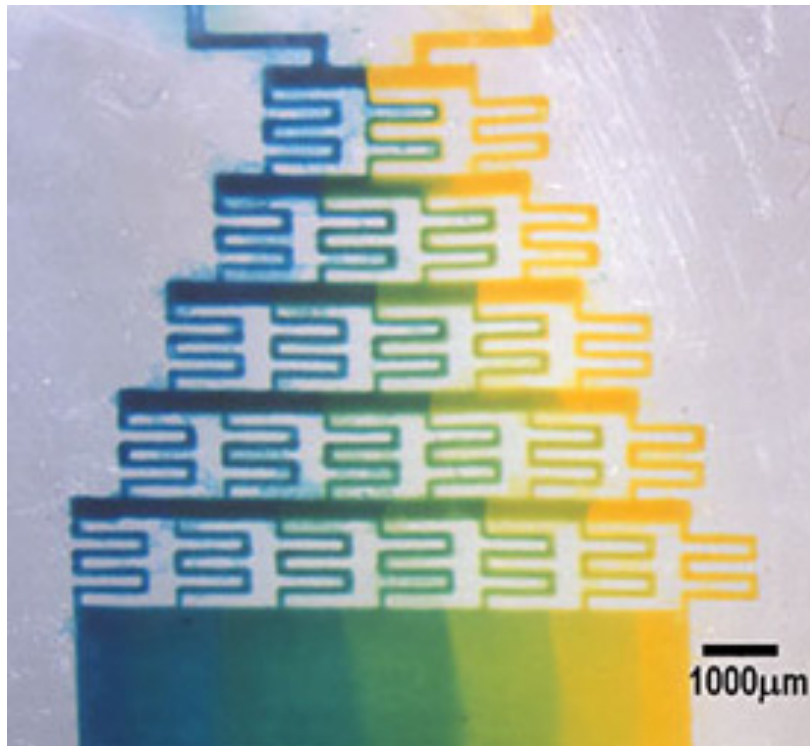
Integration of the rapid mixer

Accelerated 10X

Sensoreal 2014

# Paper microfluidics

Use of a network of hydrophilic fibres to generate a flow



# Paper microfluidics

Use of a network of hydrophilic fibres to generate a flow



**Mixer**

# Electrowetting

Droplets microfluidics

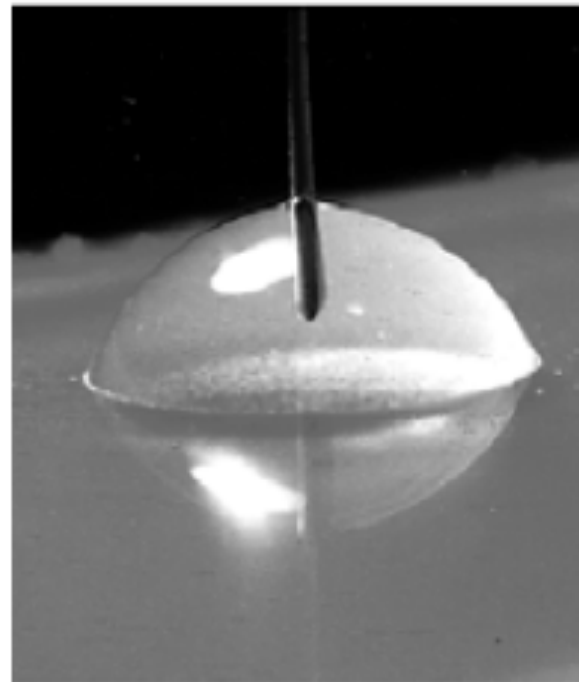
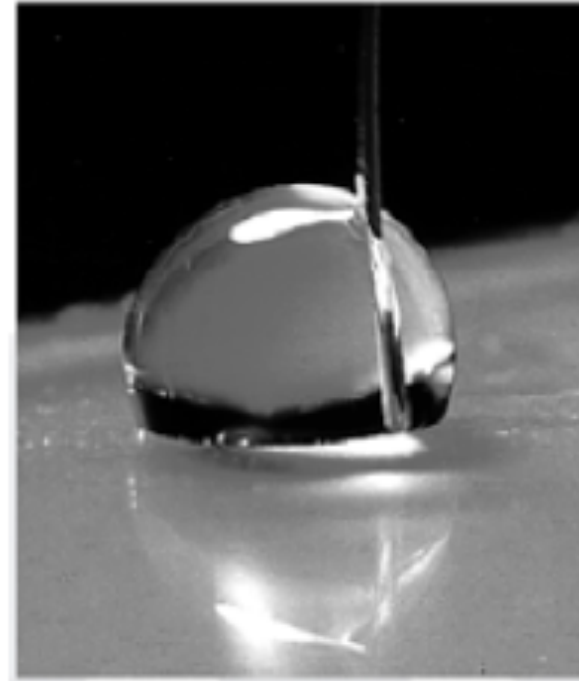
Phenomenon :

Change in wetting angle by the polarisation of a droplet on an hydrophobic surface on top of an electrode

Gabriel Lippman

Nobel price 1908

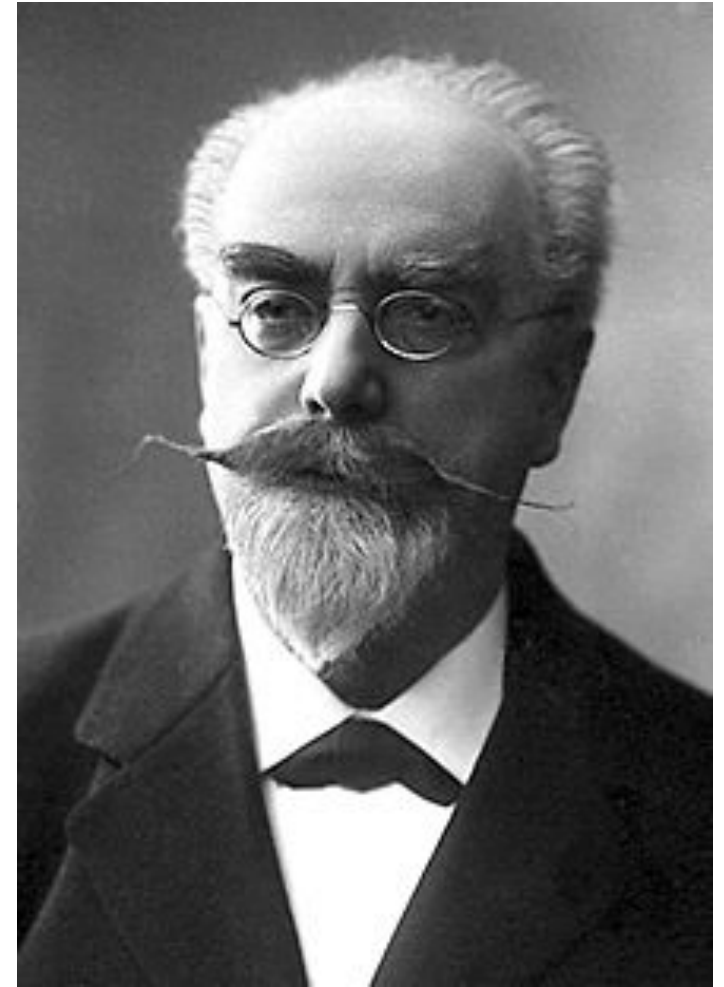
M.G. Lippmann, "Relation entre les phénomènes électriques et capillaires." Ann. Chim. Phys, 5:494, 1875



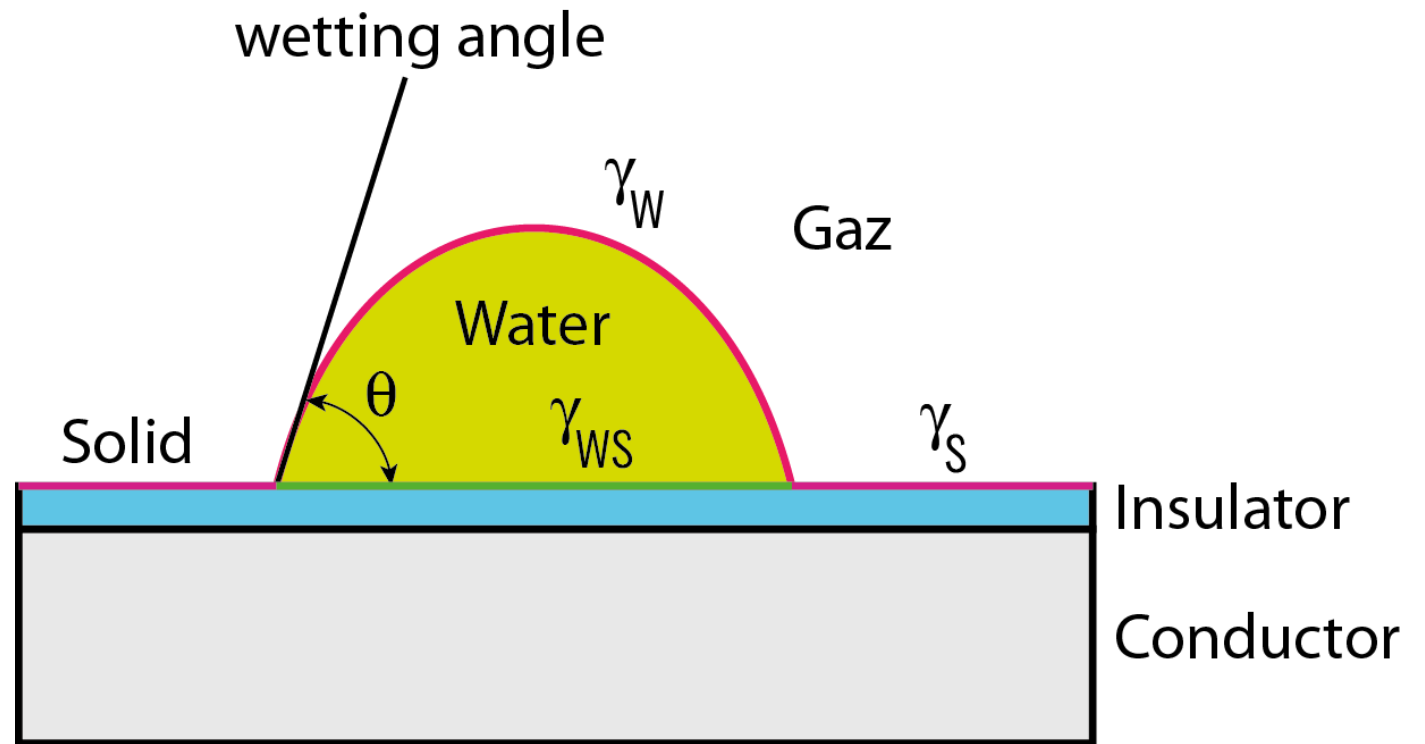
# Gabriel LIPPMAN

**Jonas Ferdinand Gabriel Lippmann** (16 août 1845 - 13 juillet 1921)

est un physicien français. Il est lauréat du prix Nobel de physique de 1908 « pour sa méthode de reproduction des couleurs en photographie, basée sur le phénomène d'interférence ». Sa découverte permet la reconstitution intégrale de l'ensemble des longueurs d'onde réfléchies par un objet. (wikipedia)



# Electrowetting



Young-Dupré equation

$$\gamma_{ws} = \gamma_s - \gamma_w \cos(\theta)$$

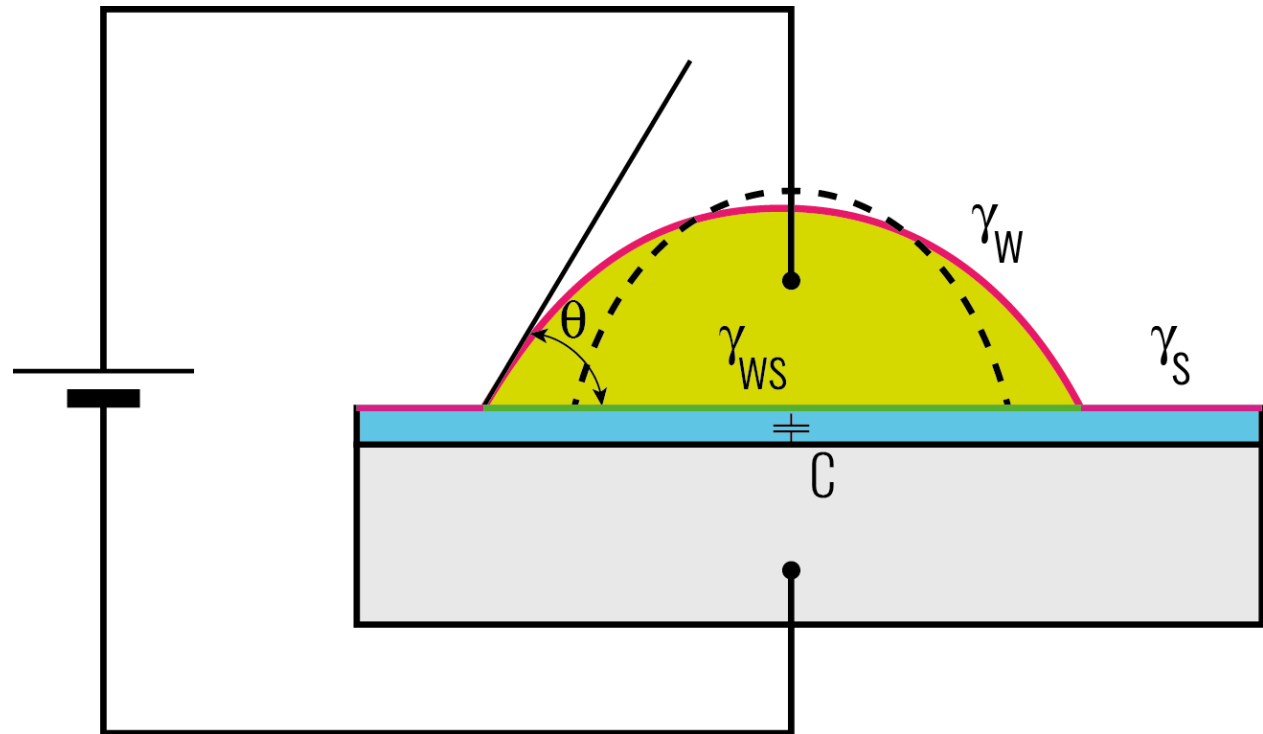
# Electrowetting

Lippman equation

$$\gamma_{ws} = \gamma_{ws}^0 - \frac{CV^2}{2}$$

$$C = \frac{\epsilon_0 \epsilon_r S_{SL}}{d}$$

$$\cos(\theta) = \frac{\gamma_s - \gamma_{ws}^0 + \frac{CV^2}{2}}{\gamma_w}$$

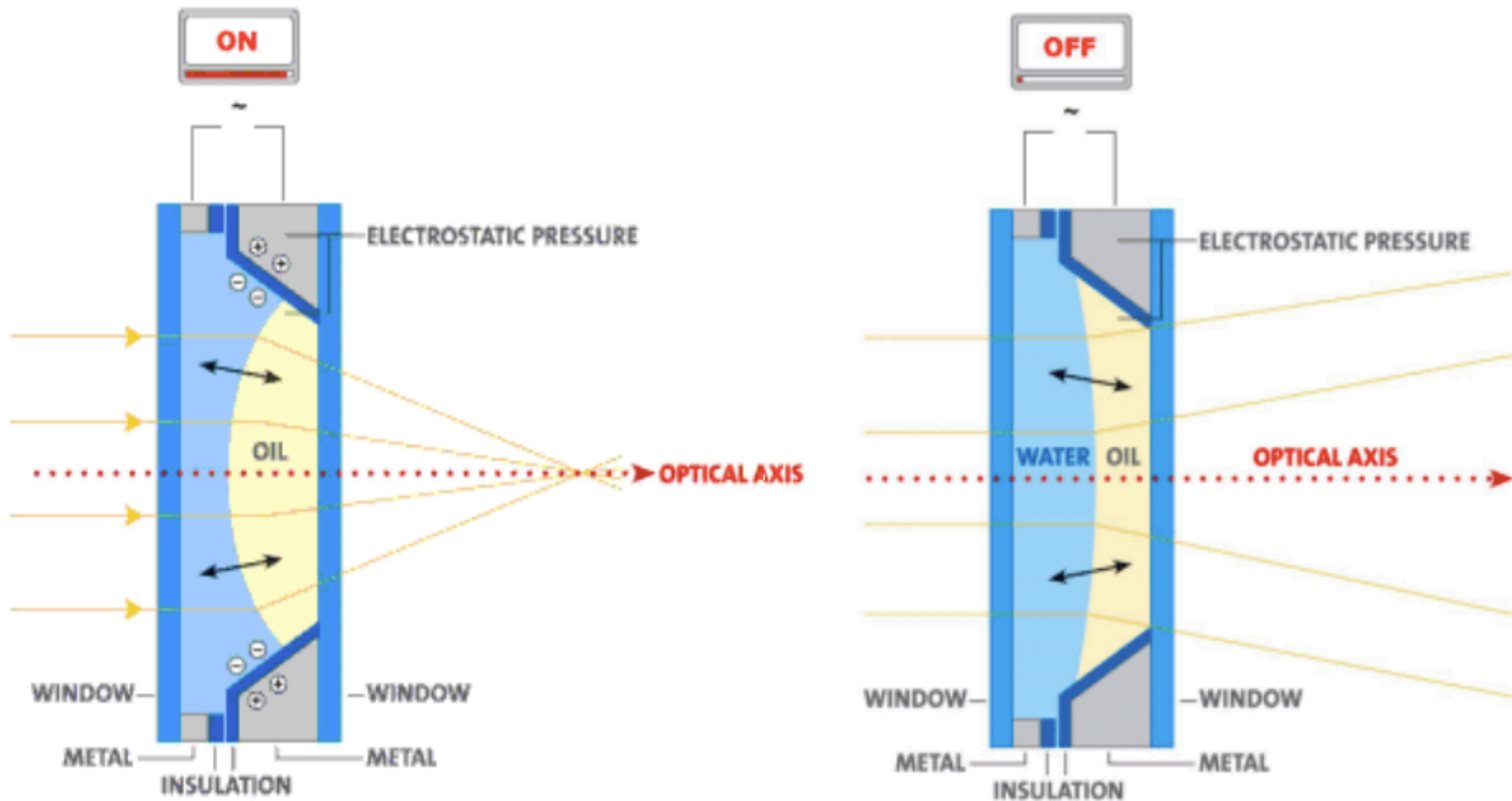


When voltage increases the wetting angle decreases, the droplet smashes

There is a saturation regime

# Electrowetting

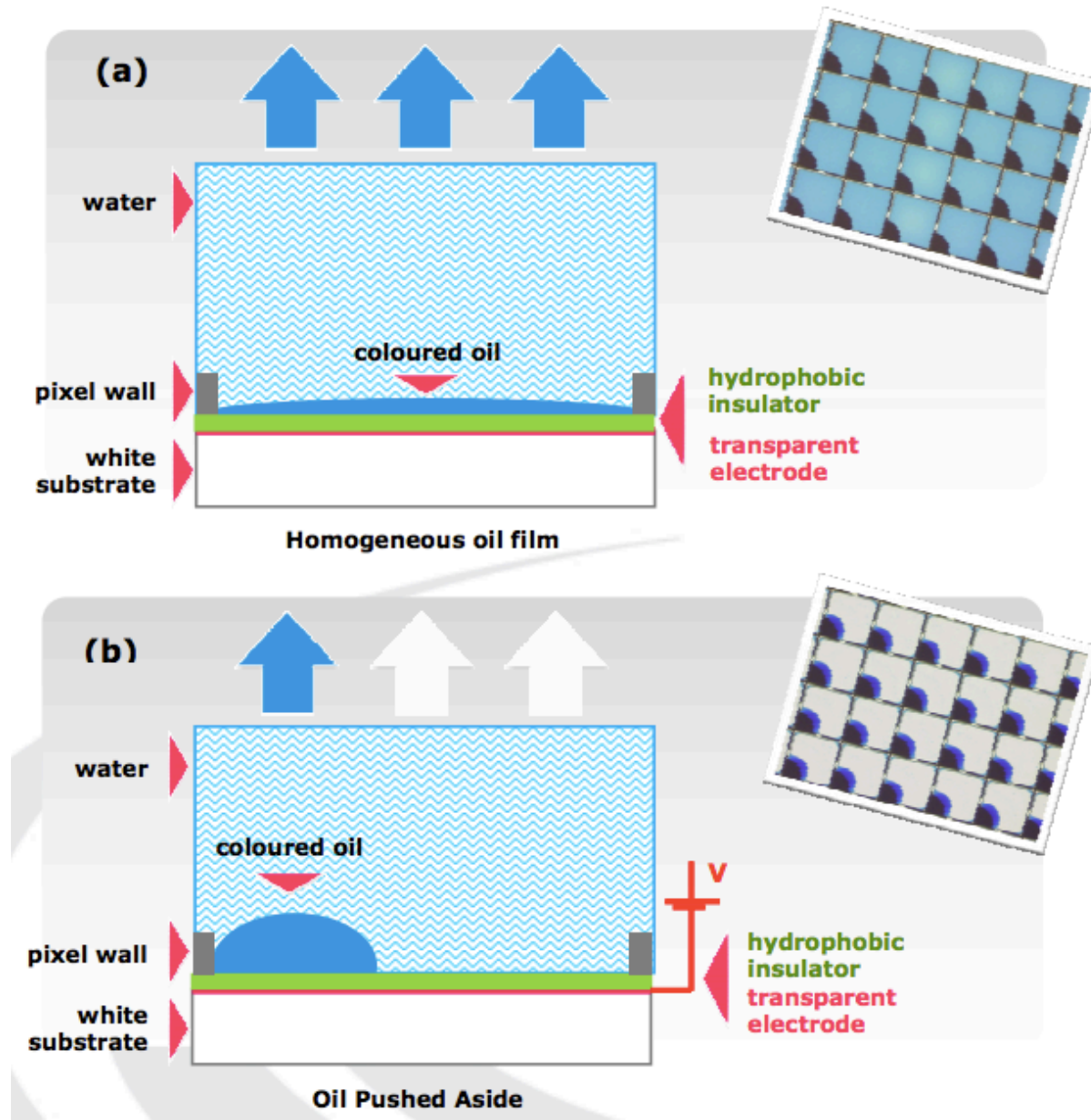
Application : variable focus lenses





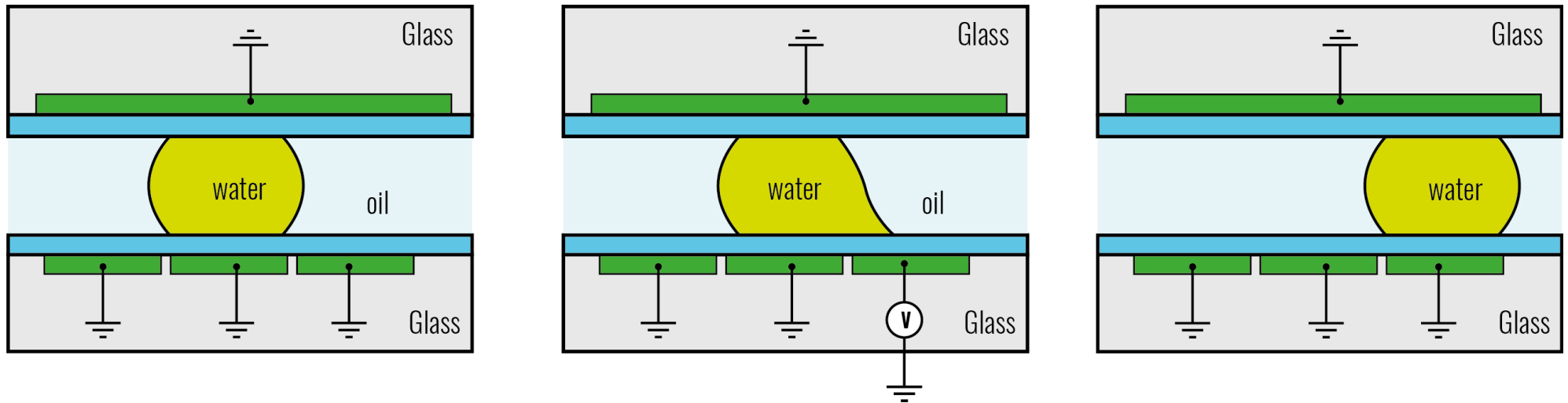
# Electrowetting

Application : flat screens



# Electrowetting

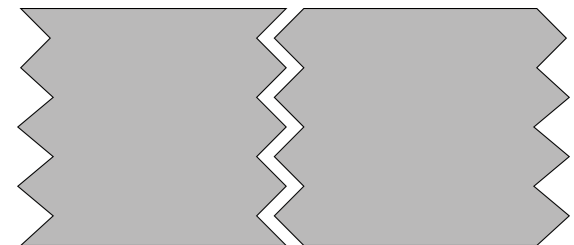
How to move a droplet ?



To avoid evaporation : droplet caught between glass blades + oil encapsulation

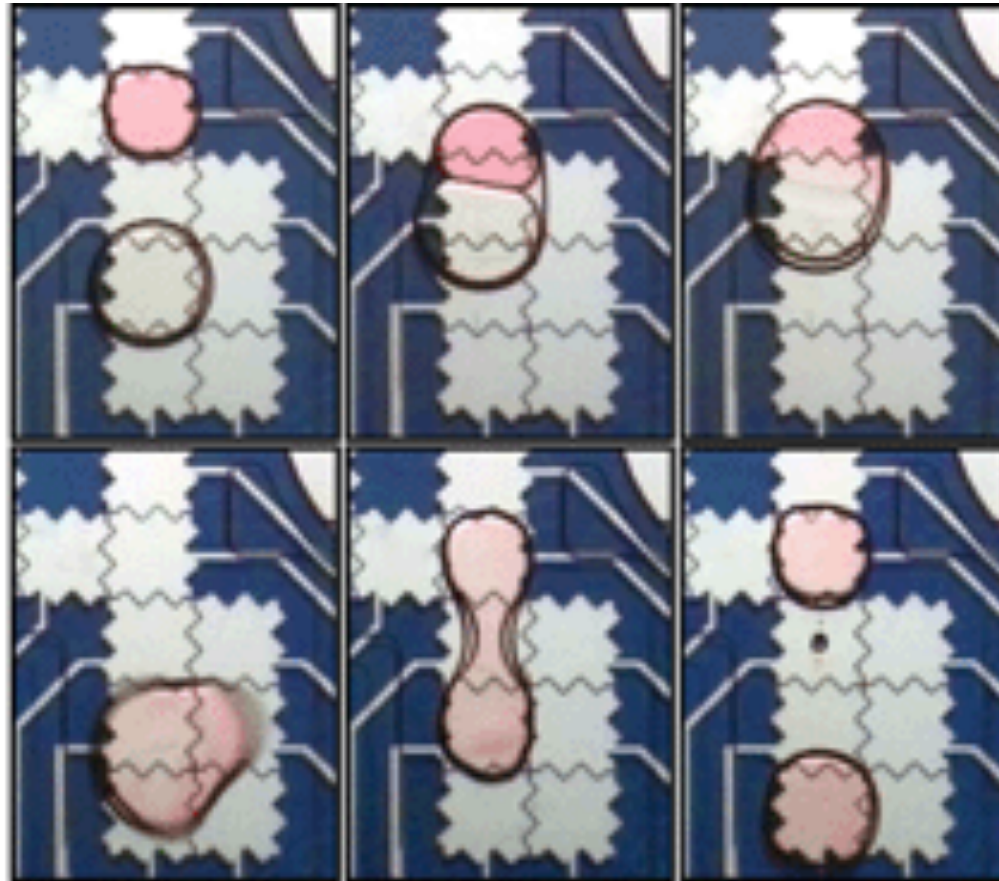
Contact angle modification near one cell border -> global movement of the droplet from one cell to another

! Requires overlapping electrodes



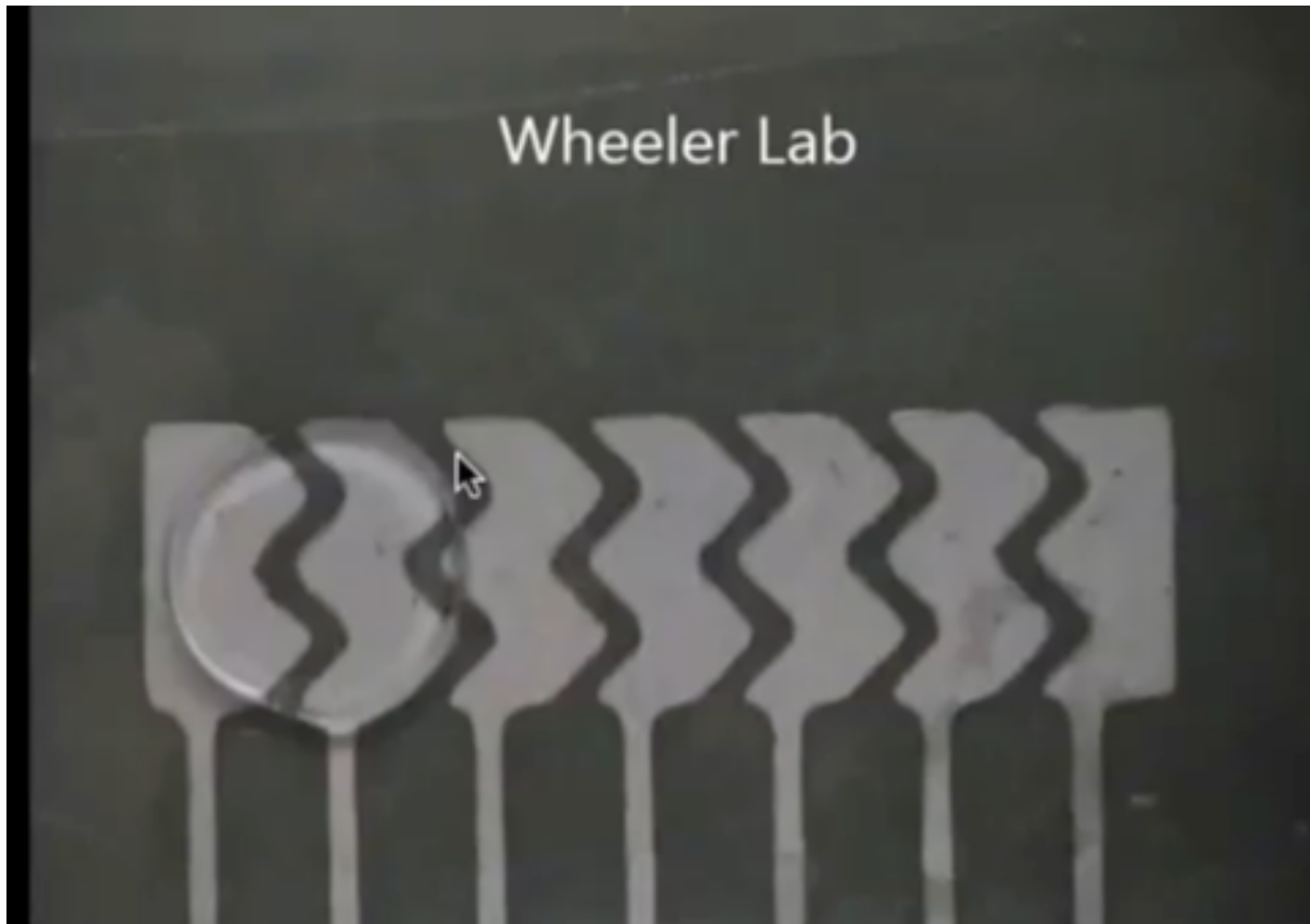
# Electrowetting

How to move a droplet ?

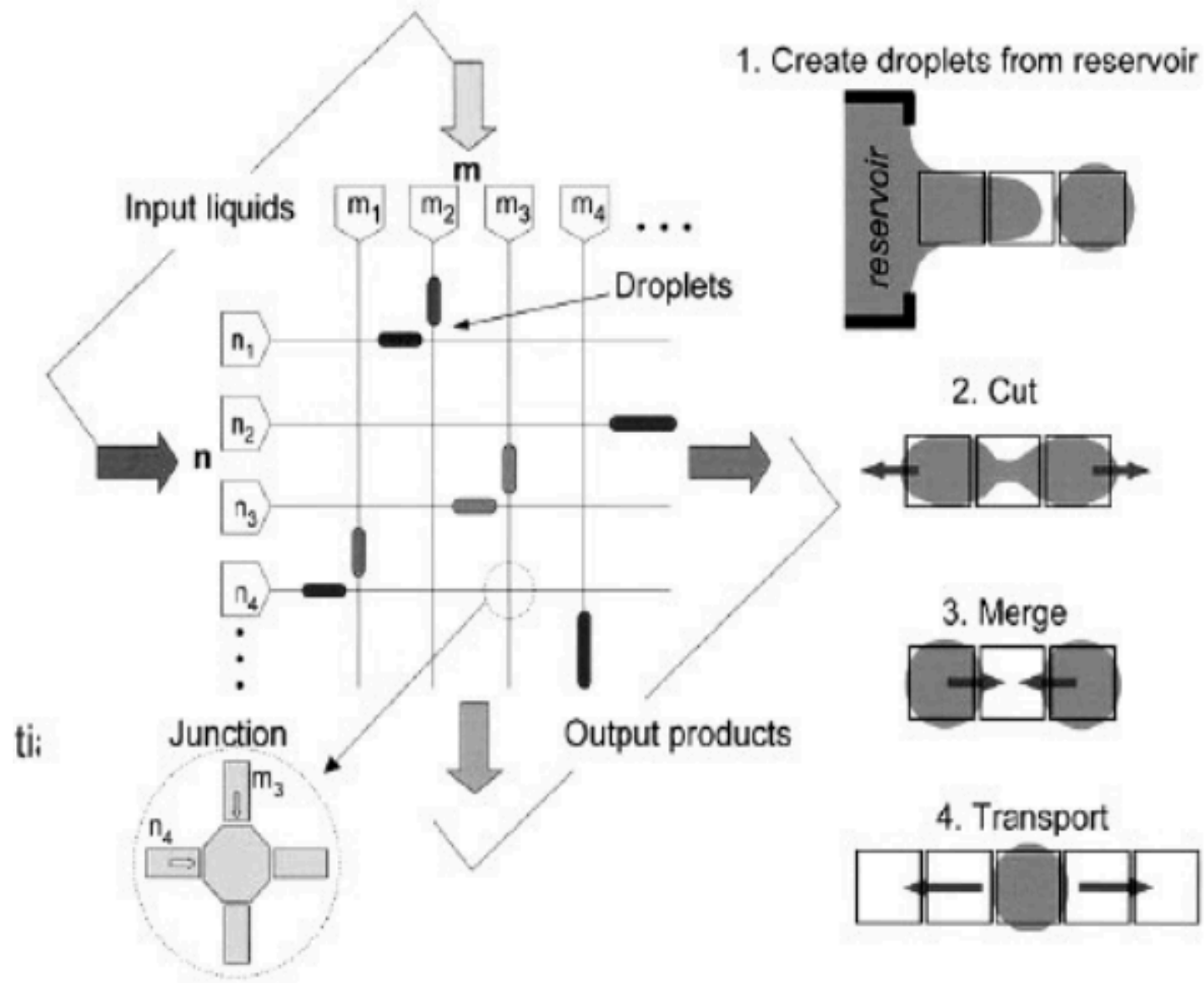


# Electrowetting

How to move a droplet?



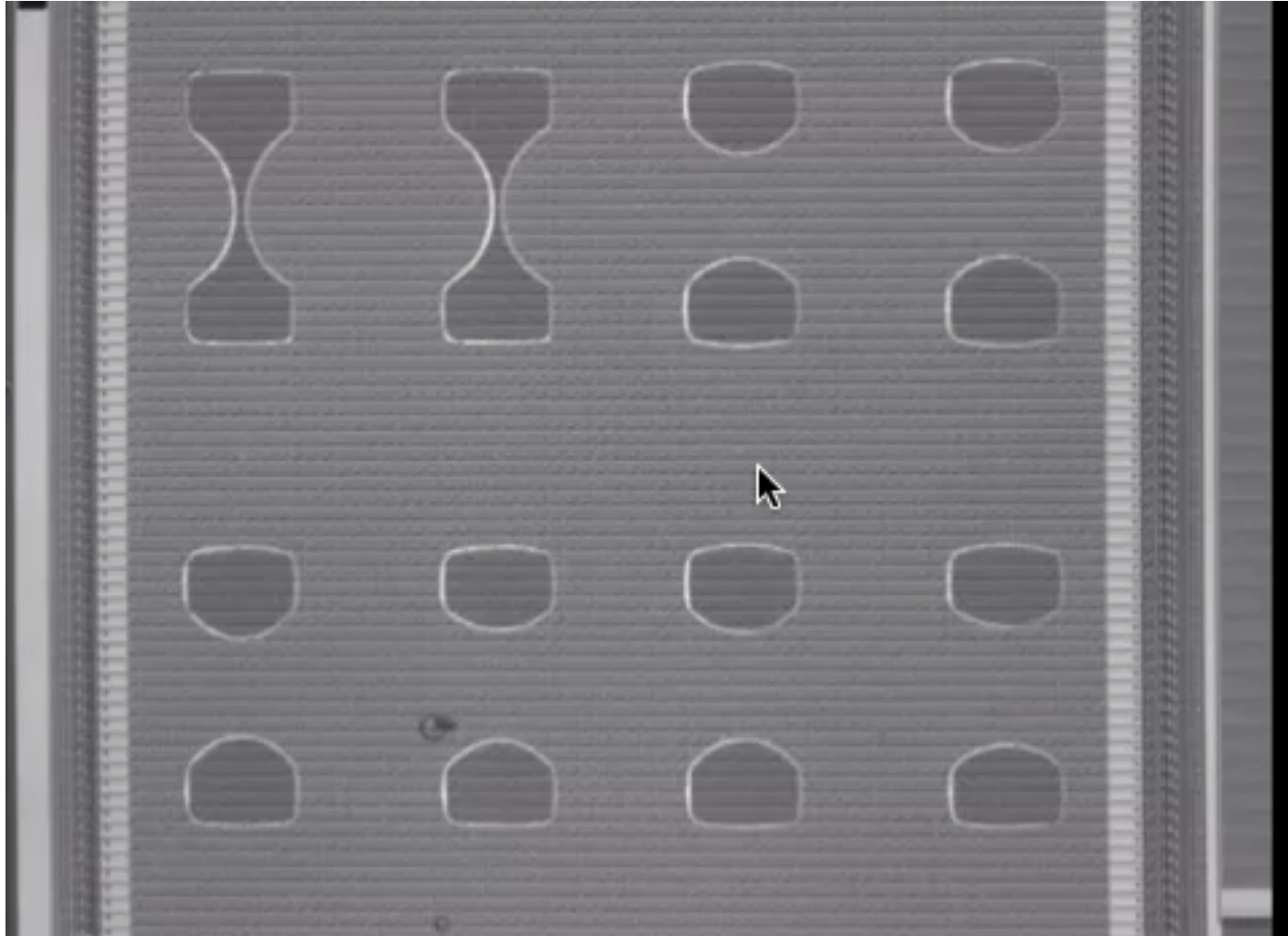
# Electrowetting



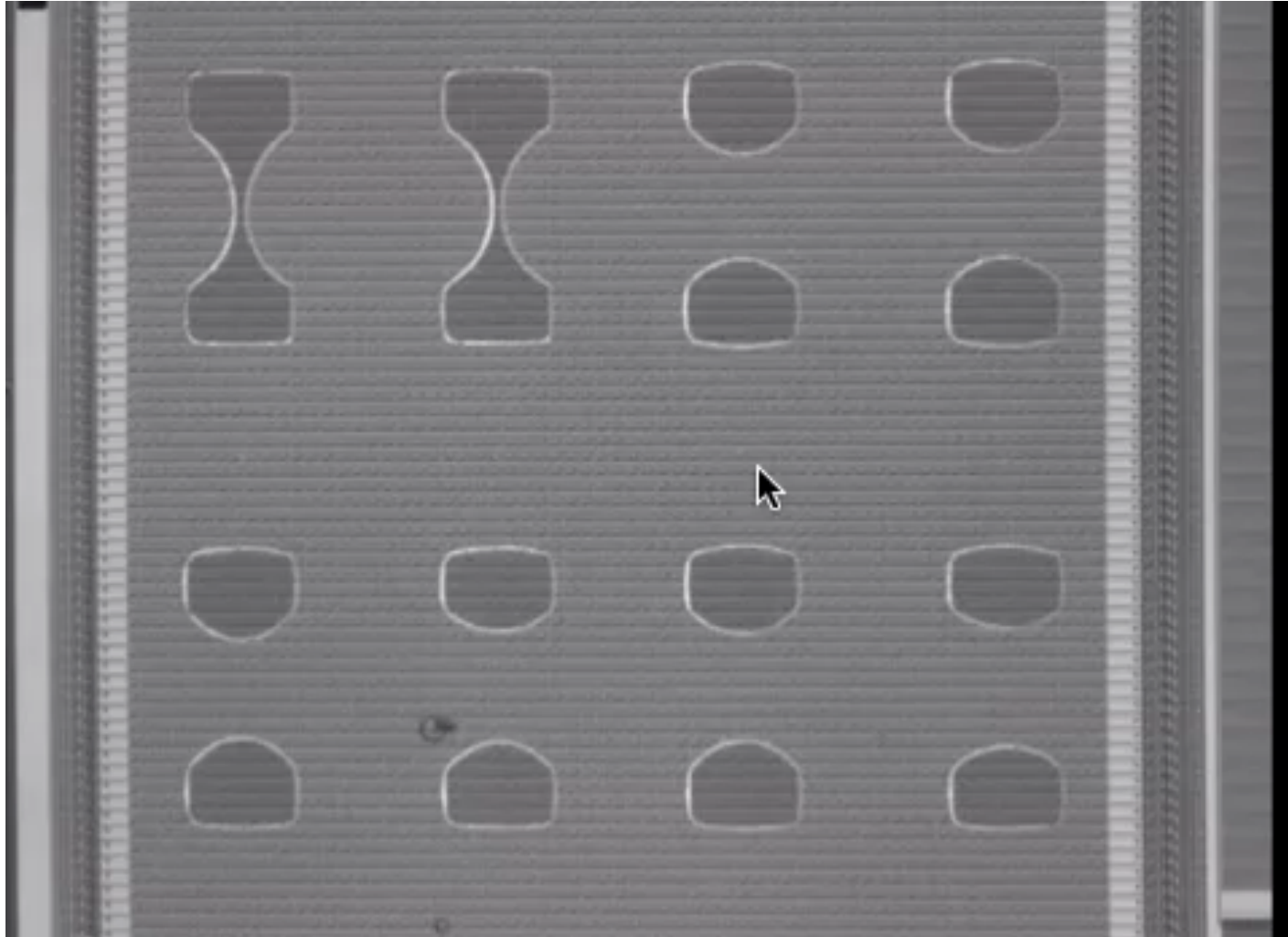
# Electrowetting

Droplet  
manipulations

# Electrowetting

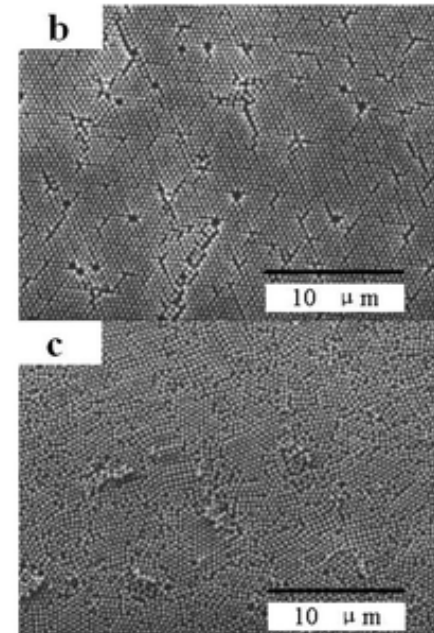
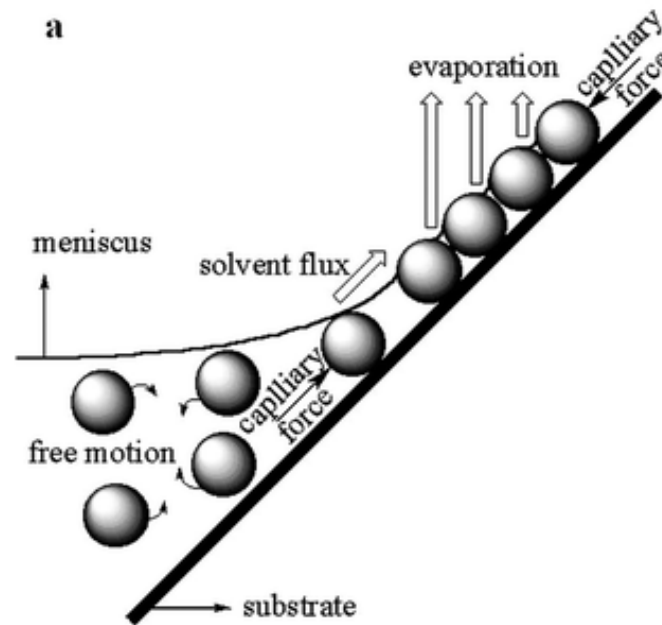
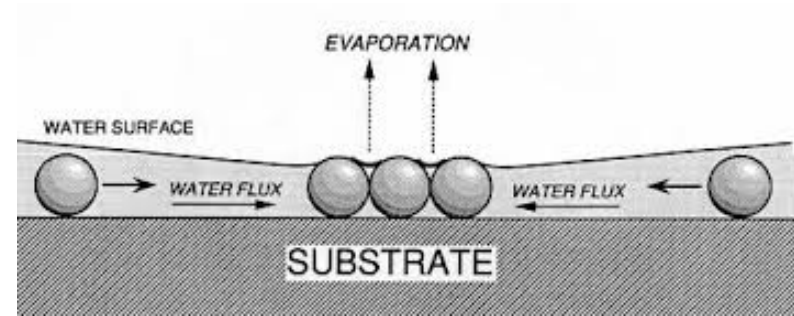
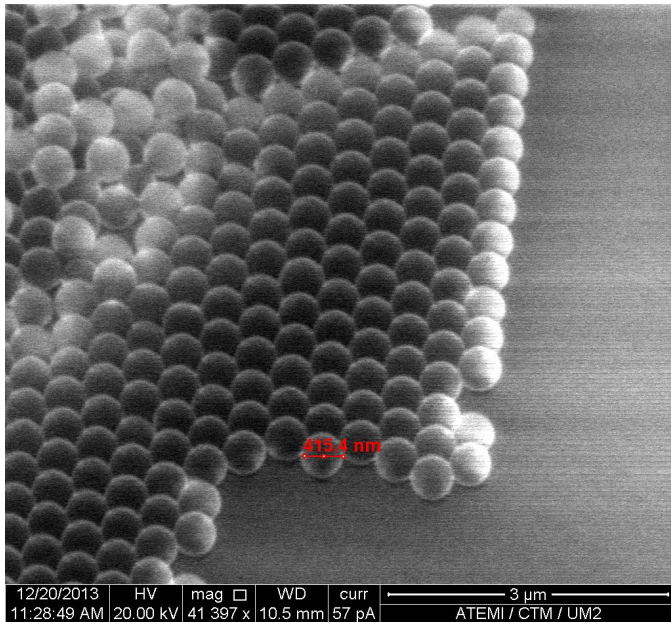
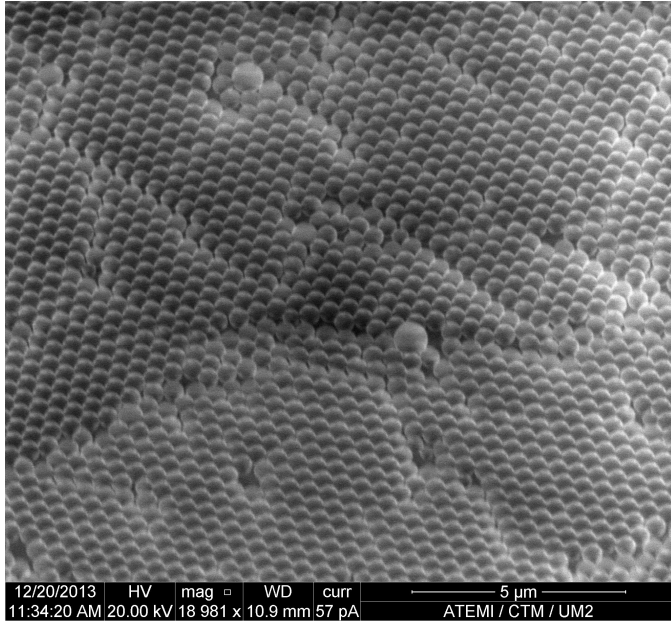


# Electrowetting



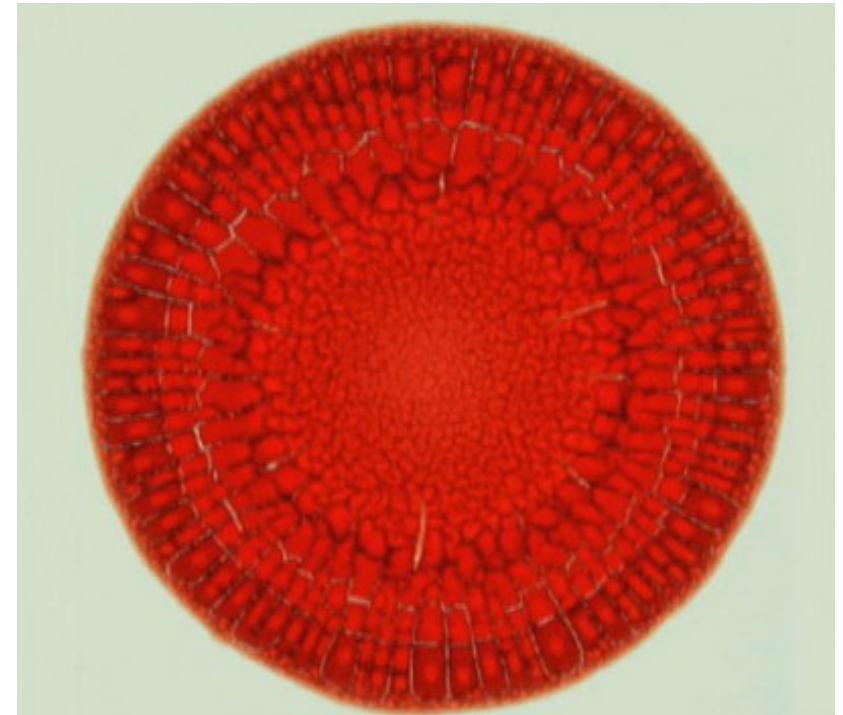
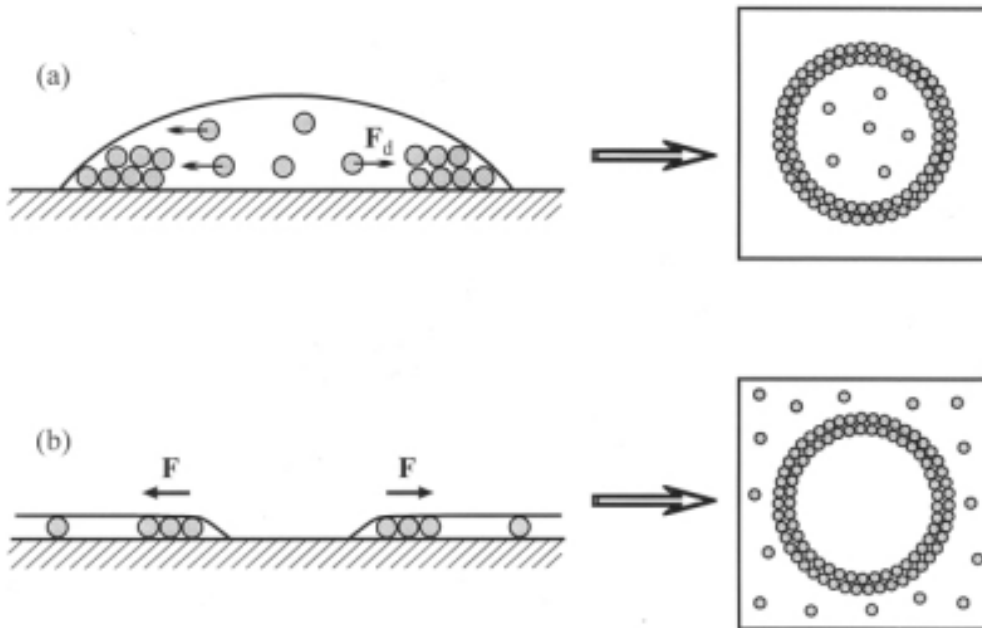


# Capillary Force Assembly

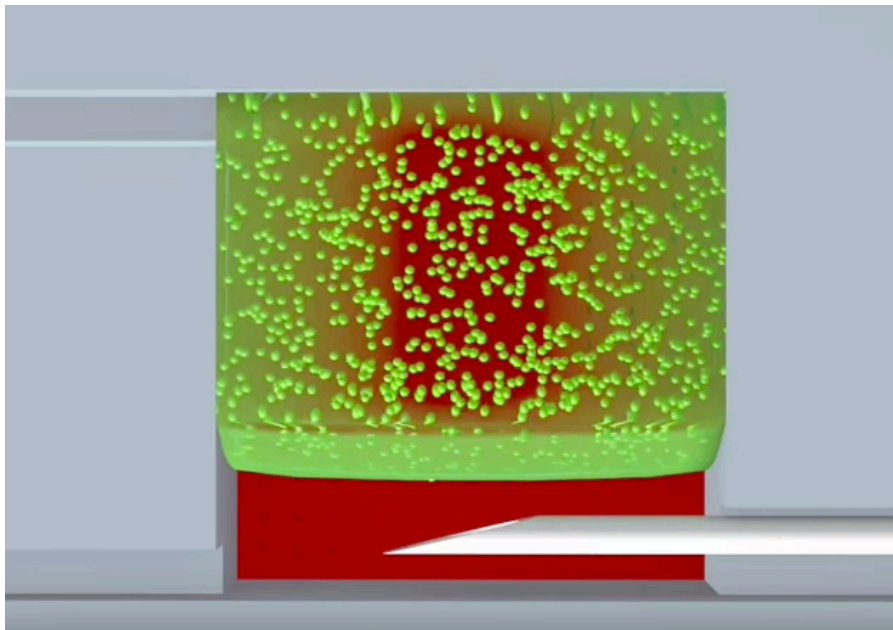


# Capillary Force Assembly

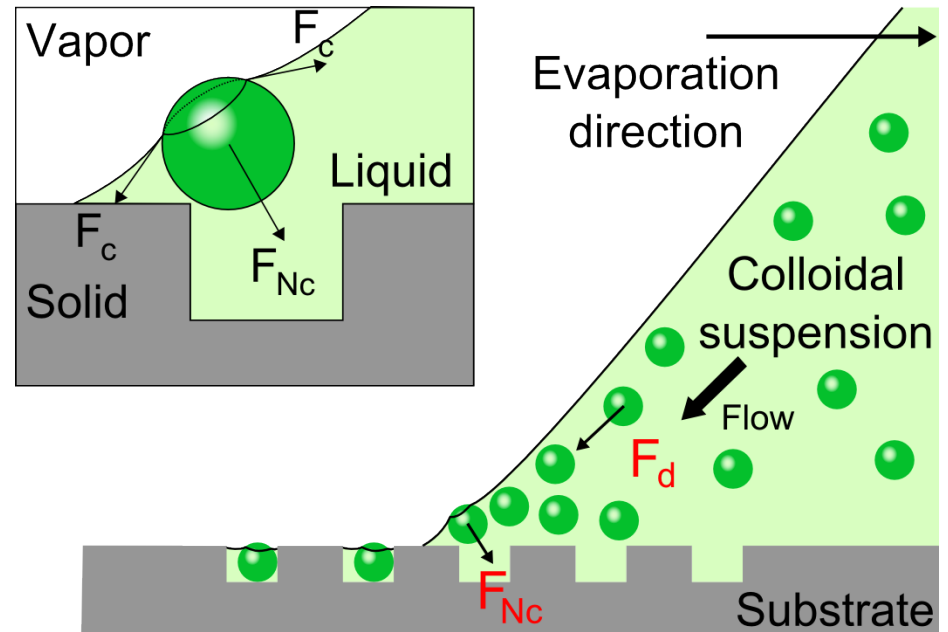
Capillary force assembly : interactions between particles mediated by fluid interfaces.



# Capillary Force Assembly

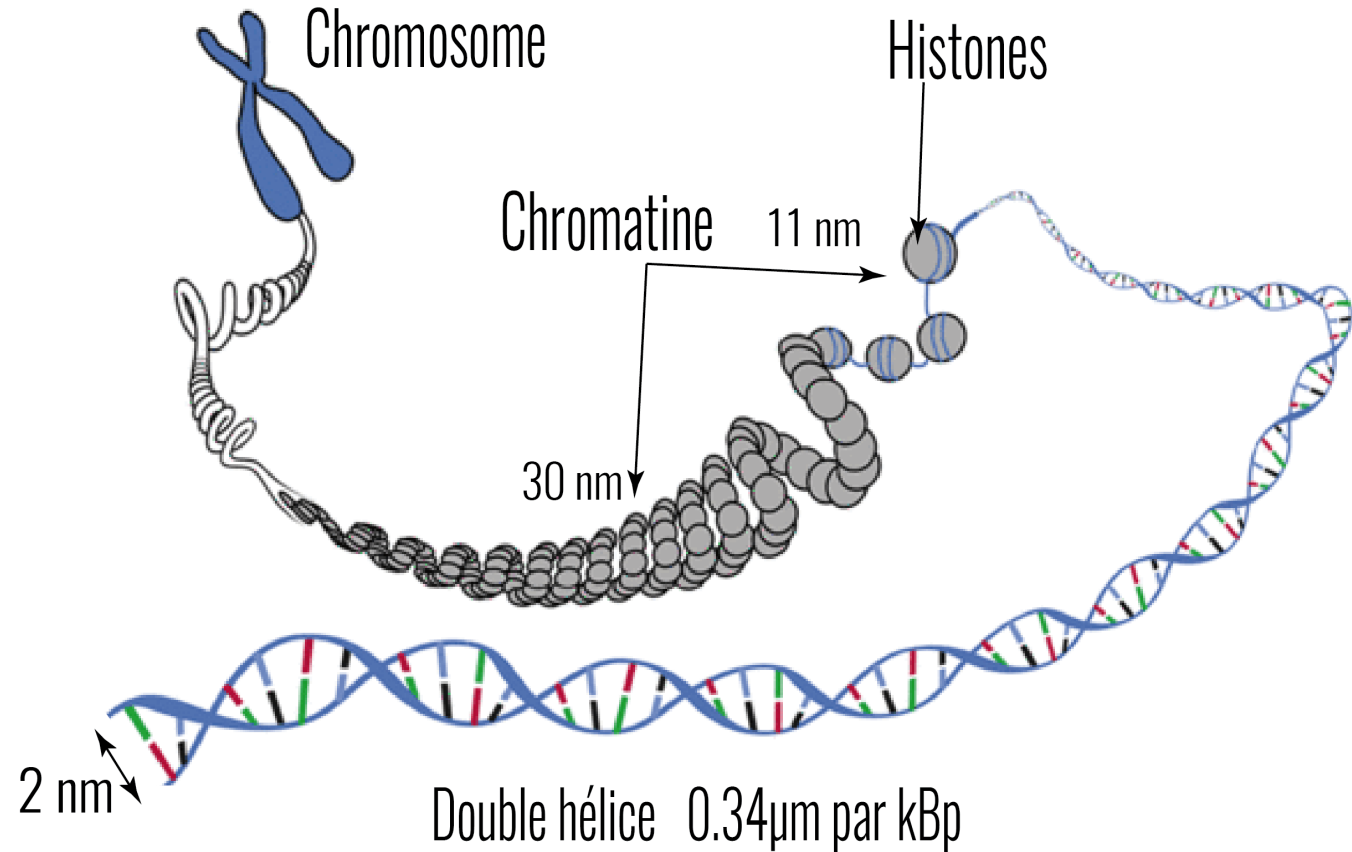


D.Peyrade, LTM



# Capillary Force Assembly : DNA Combing

→ DNA organisation



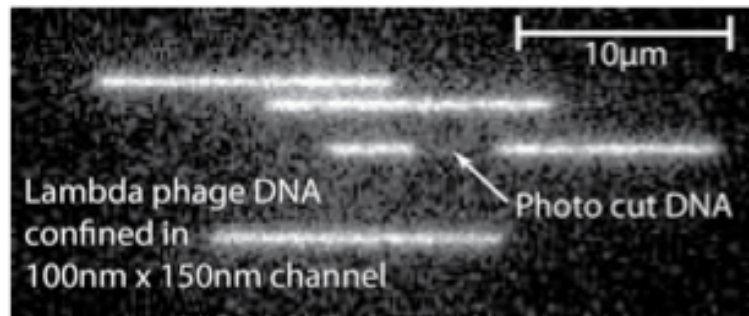
Persistence length: 100 nm for dsDNA and 2 nm for ssDNA

In solution : Pellets, Coiling

# Capillary Force Assembly : DNA Combing

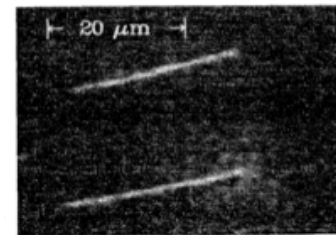
How to uncoil DNA ?

→ Nanofluidic containment

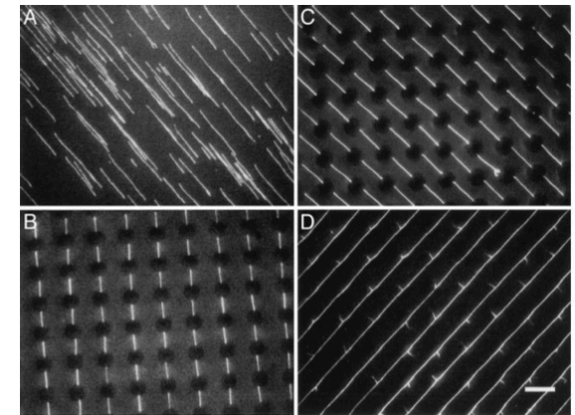


F. Westerlund, Chalmers

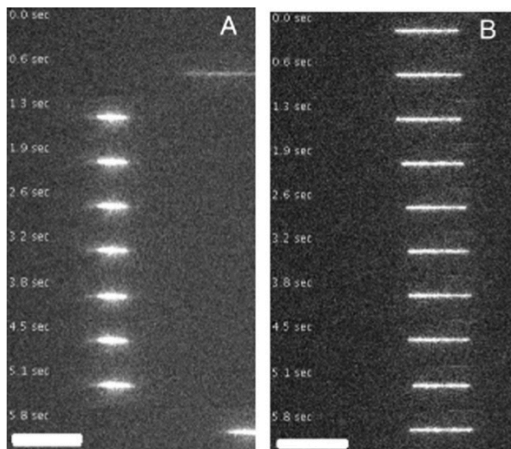
→ Deposition by dewetting



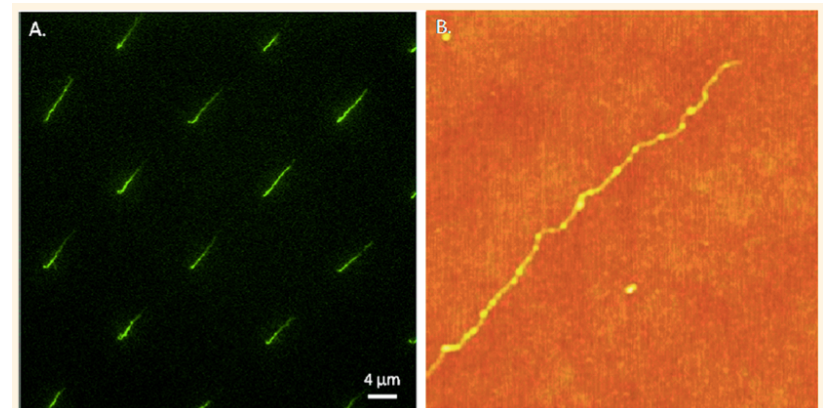
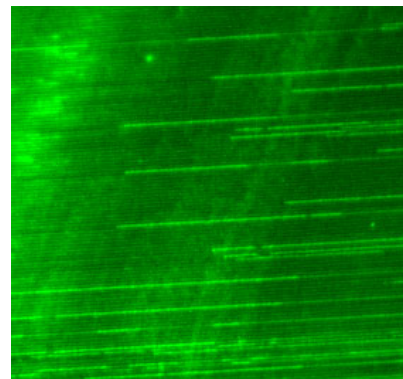
D. Bensimon, ENS



J. Guan and L. J. Lee Ohio State University



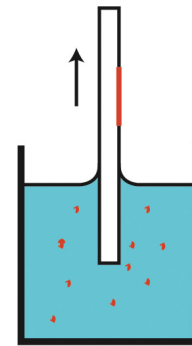
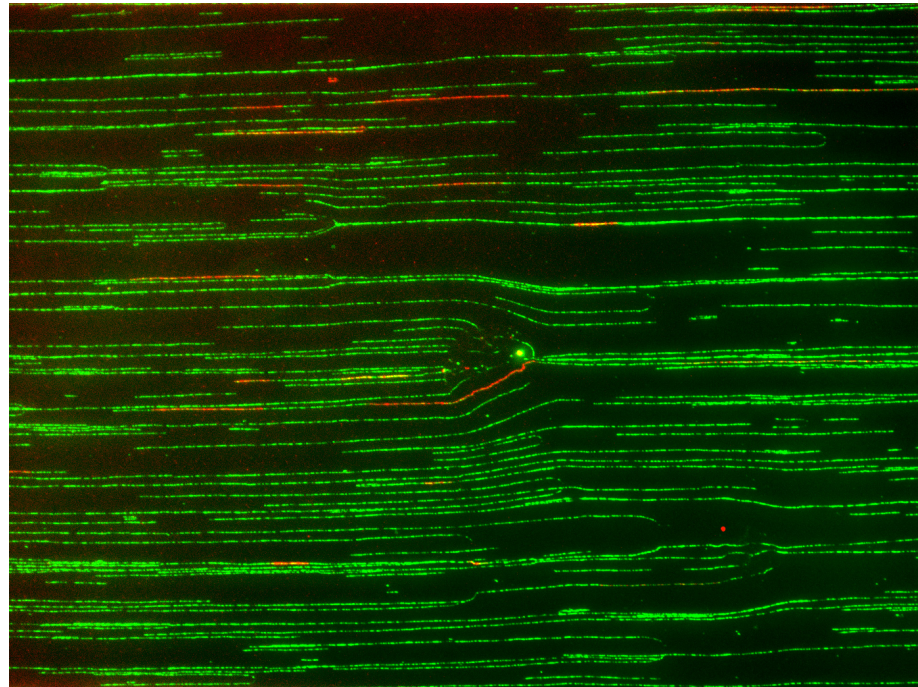
D.E. Streng; North Carolina state Univ.



A. Cerf, LAAS CNRS

# Capillary Force Assembly : DNA Combing

The standard DNA combing technique used everyday at IGMM



Human genomic DNA, YOYO tagged, 237 x 177  $\mu\text{m}$  image

Substrate Silanization

DNA ends anchoring at pH 5,4

Slow dewetting

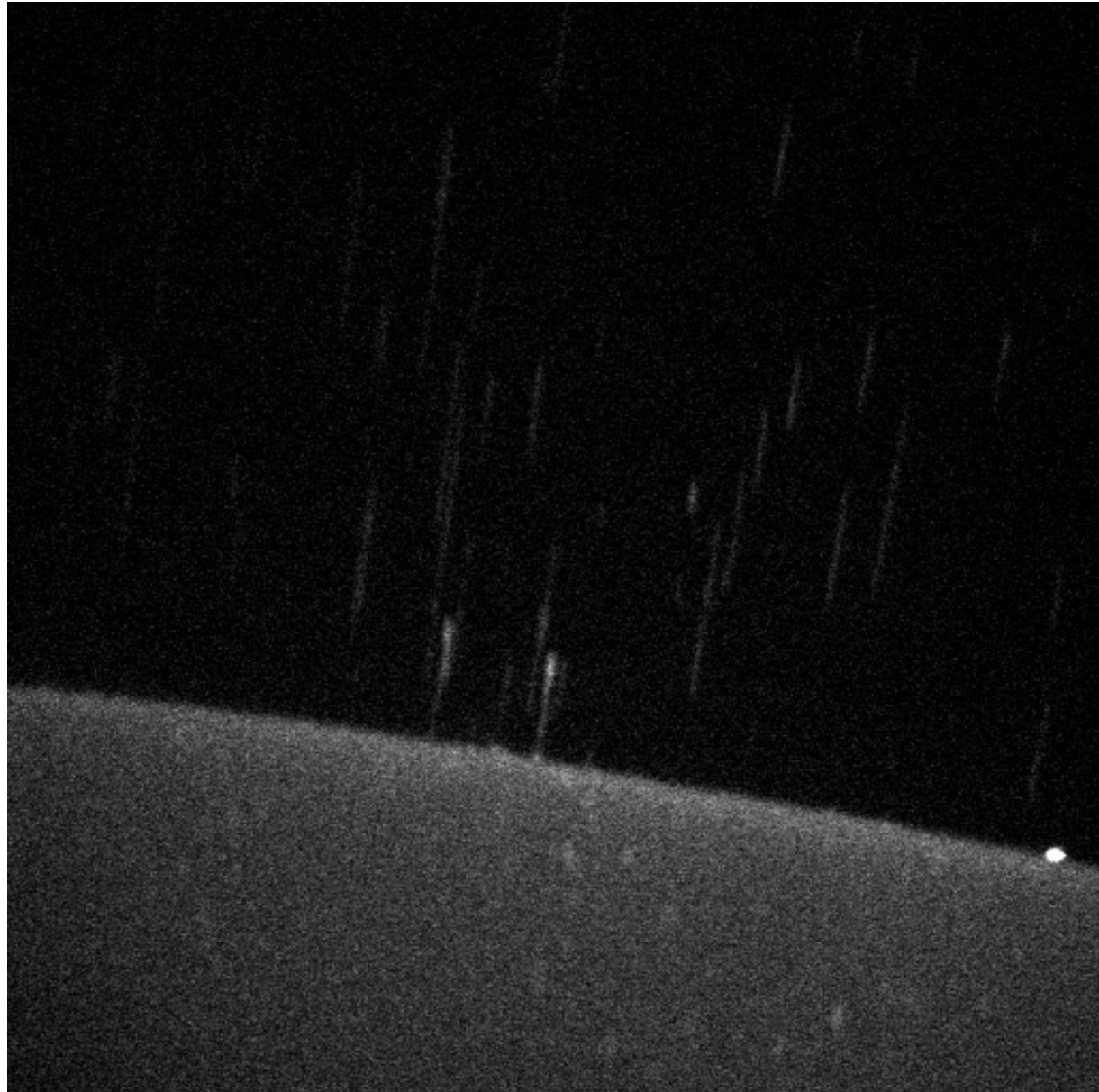
# Capillary Force Assembly : DNA Combing

Combing of Genomic DNA from Droplets Containing Picograms of Material

Jochem Deen, Wouter Sempels, Raf De Dier, Jan Vermant, Peter Dedecker, Johan Hofkens, and Robert K. Neely

ACS Nano 2015 9 (1), 809-816

DOI: 10.1021/nn5063497



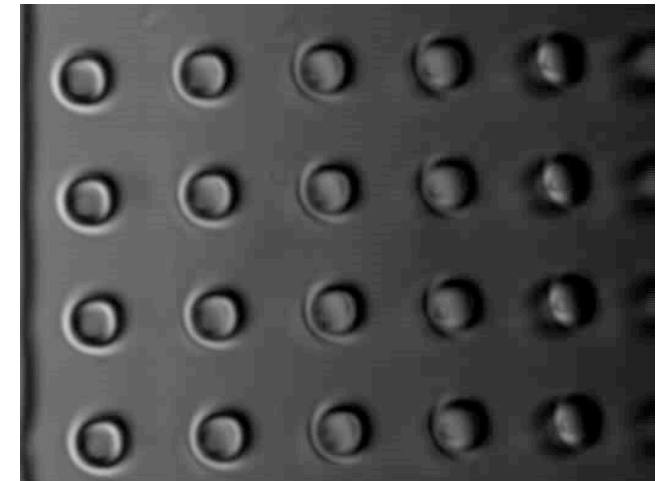
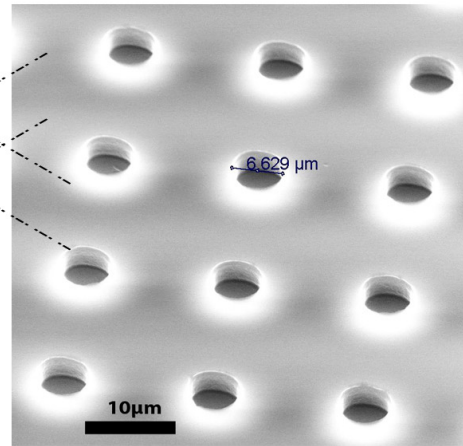
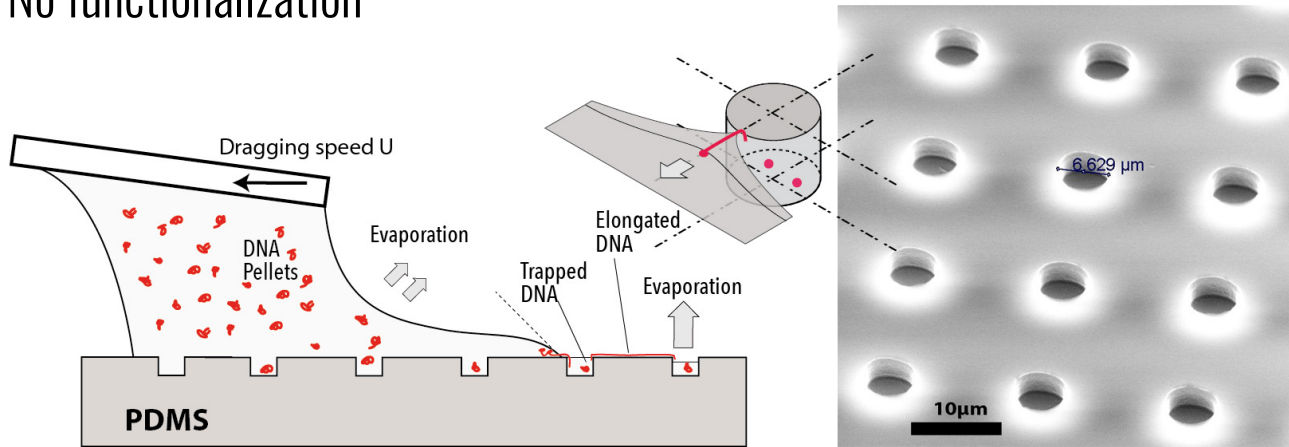
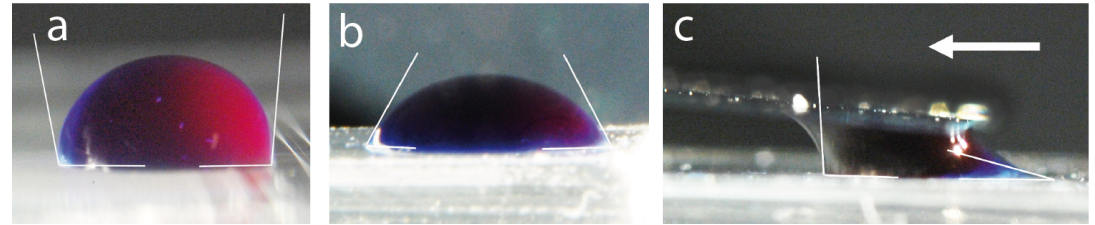
# Capillary Force Assembly : DNA Combing

Ordered deposition

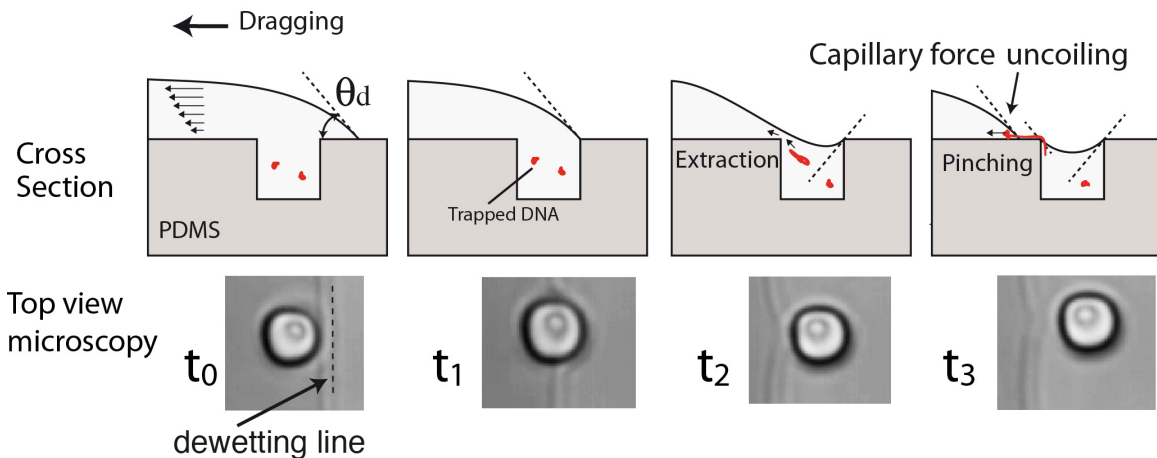
Forced dewetting on perturbations

PDMS substrate

No functionalization

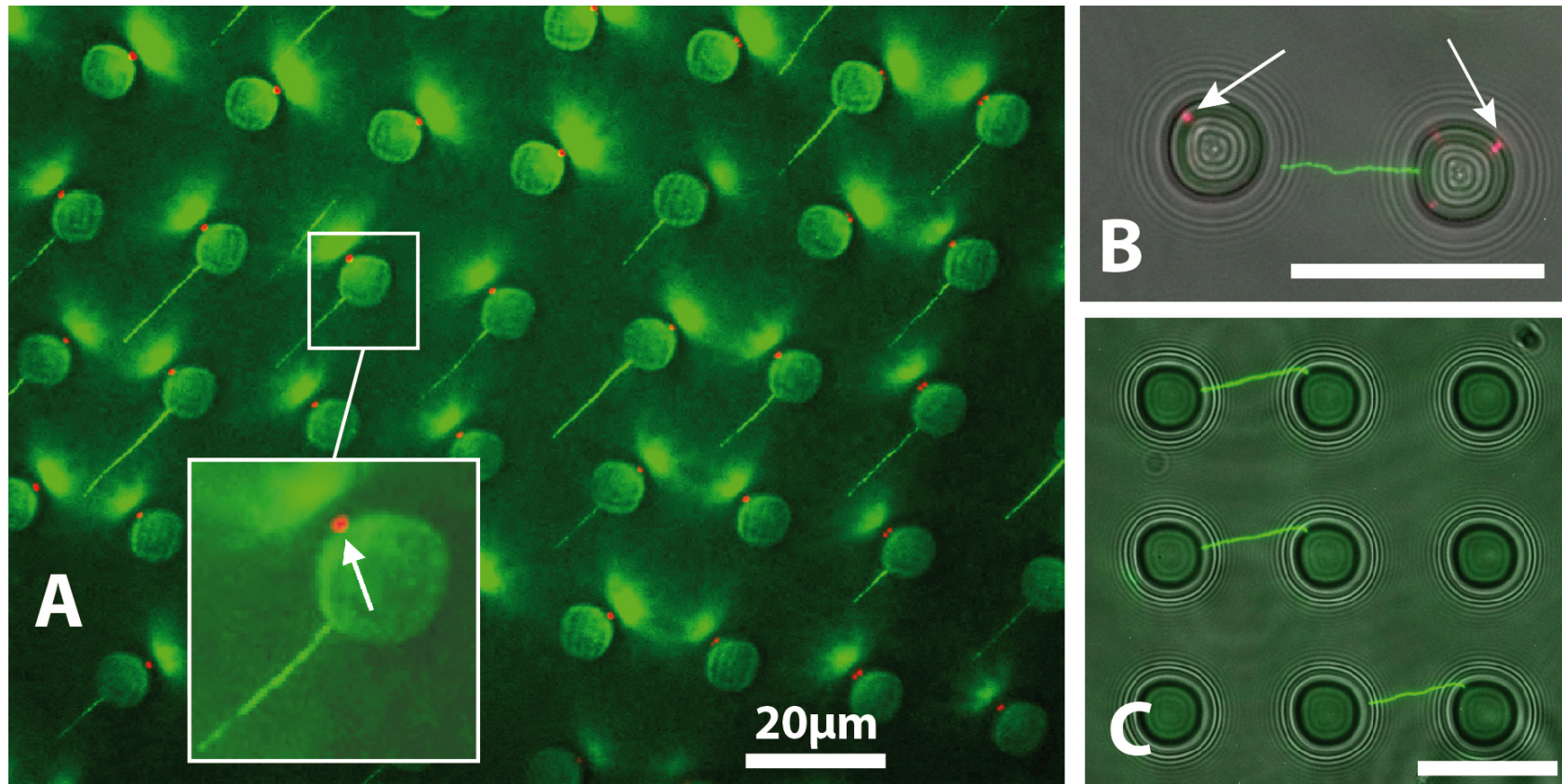


4/4/2013 11:36:18 AM -00:00:01:775.97[HH:MM:SS:mm] 000007558  
880x617 998fps 697μs





# Capillary Force Assembly : DNA Combing



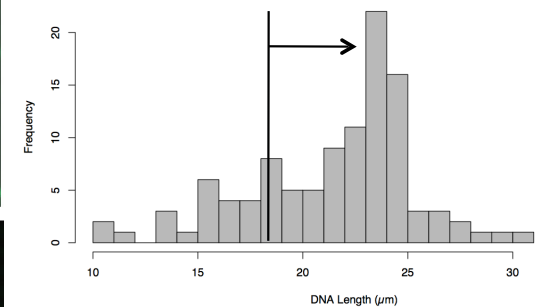
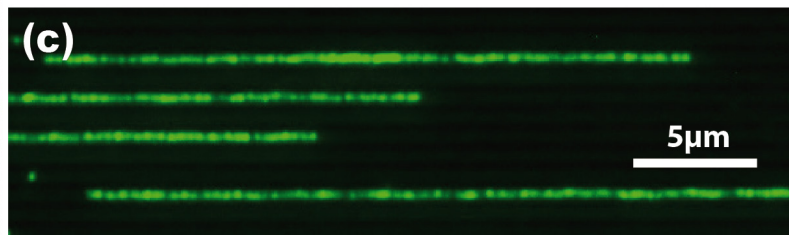
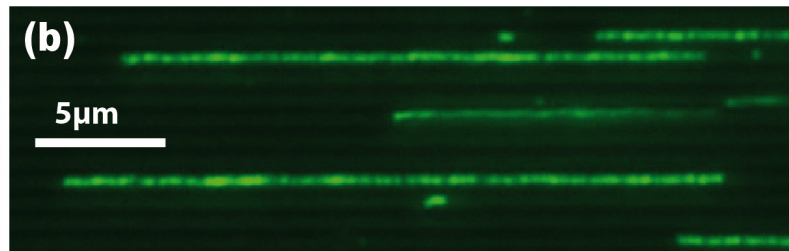
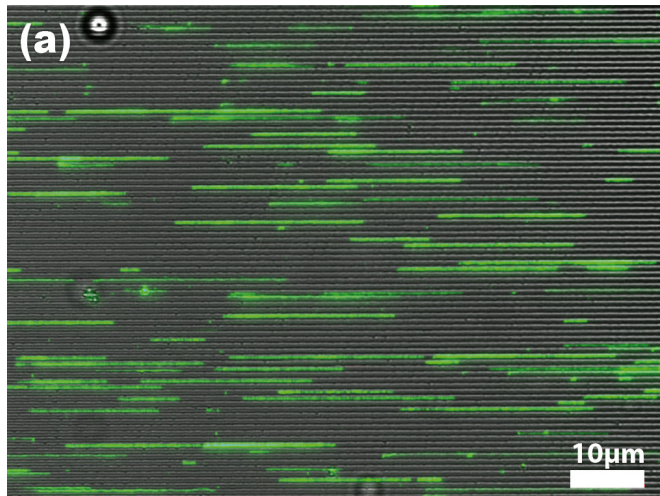
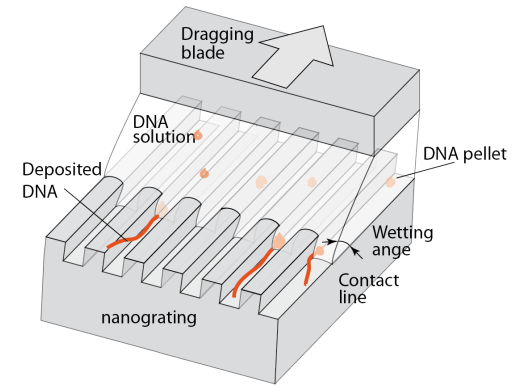
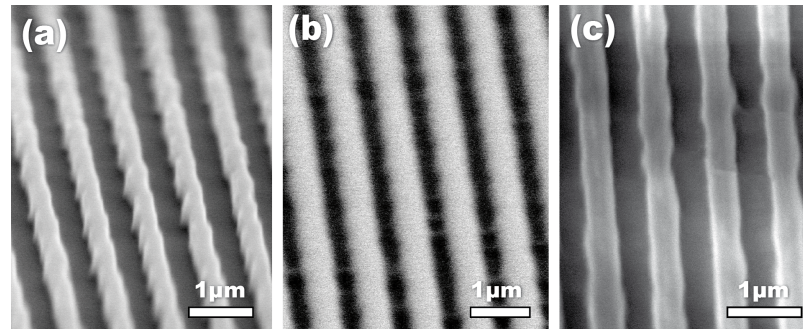
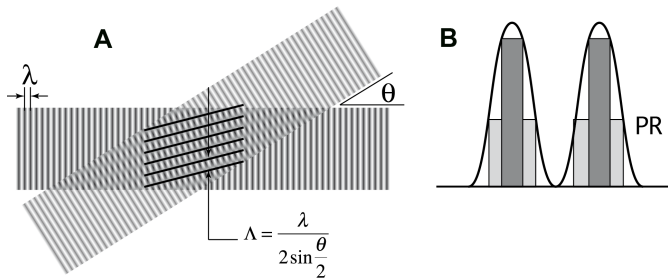
composite Image (GFP Fluorescence + transmitted light) of  $\lambda$  phage DNA (48kbp) tagged with YOYO intercalating dye. Dewetting 400 $\mu$ m/s. Red: uncoiled DNA pellets, 5 $\mu$ m below surface

B. Charlot, et al. "Elongated unique DNA strand deposition on microstructured substrate by receding meniscus assembly and capillary force", *Biomicrofluidics* 8, 014103 (2014).

# Capillary Force Assembly : DNA Combing

Combing on nanogratings : rectilinear conformation

800nm pitch nanogratings : Interference lithography



Stretching ratio 150%